

*Regional Cooperation for
Limited Area Modeling in Central Europe*



On Refining the Vertical Resolution of Numerical Weather Prediction Models

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- ▶ The NWP community continuously seeks to benefit from increased Δx (adapting the physical processes and exploiting high-resolution surface/observations datasets), while Δz typically remains unchanged
- ▶ Main reason: necessity of lowering the First Model Level (FML). If placed considerably below 10-m without adjustments: possible violation of Monin-Obukhov Similarity Theory (MOST), increased sensitivity to surface dataset errors, coupling inconsistencies with the upper-air turbulence scheme, numerical stiffness, etc.
- ▶ This presentation focuses on aspects related to the turbulence scheme and builds on the discussion from the Autumn Surface Working Week 2023

- MOST is a scaling theory for the surface layer of the PBL (based on several characteristic scales; L , u_* and s_*):

$$\frac{\kappa(z + z_{0m})}{u_*} \frac{du}{dz} = \phi_m \left(\frac{z + z_{0m}}{L} \right) \xrightarrow{\text{integr.}} u(z) = \frac{u_*}{\kappa} \left[\ln \left(\frac{z + z_{0m}}{z_{0m}} \right) - \psi_m \left(\frac{z + z_{0m}}{L} \right) \right]$$

$$\frac{\kappa(z + z_{0h})}{s_*} \frac{ds}{dz} = \phi_h \left(\frac{z + z_{0h}}{L} \right) \xrightarrow{\text{integr.}} s(z) = s_0 + \frac{s_*}{\kappa} \left[\ln \left(\frac{z + z_{0h}}{z_{0h}} \right) - \psi_h \left(\frac{z + z_{0h}}{L} \right) \right]$$

$$L = \frac{s_0 u_*^2}{\kappa g s_*}, \quad u_* = \left[\overline{(u'w')_s}^2 + \overline{(v'w')_s}^2 \right]^{1/4}, \quad s_* = -\frac{\overline{(s'w')_s}}{u_*}$$

$$\overline{(\chi'w')_s} = C_{M/H} \sqrt{[u^2(z) + v^2(z)]} [\chi(z) - \chi_s]; \quad \chi \equiv u, v, s \text{ and } q_t$$

Assumptions: constant-flux layer, homogeneous surface and $z \gg z_{0m,h}$!

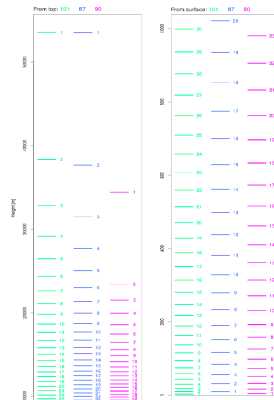
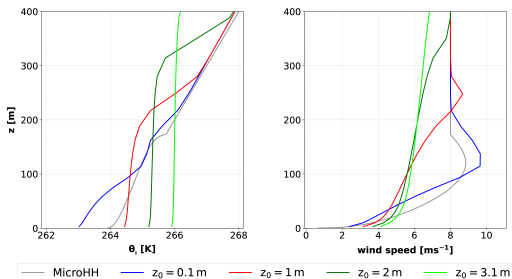
L - Monin-Obukhov length; u_*/s_* - characteristic scales; ϕ_m, h - universal similarity functions; $\psi_{m,h}$ - integrated $\phi_{m,h}$

Introduction: implementation of MOST into NWP model

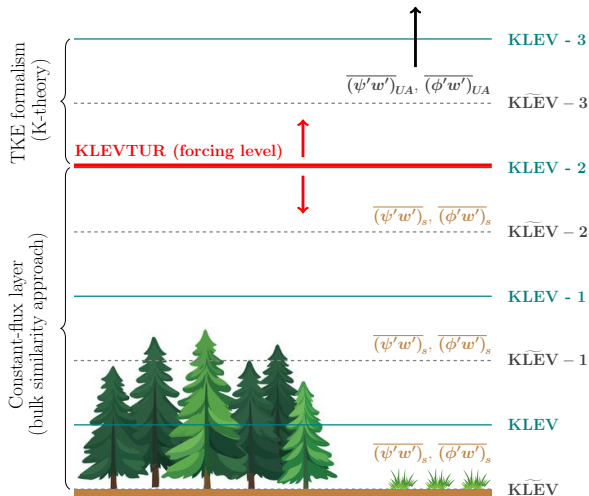
- ▶ In NWP models, a reference (forcing) height is defined ($z = Z_F$), from which atmospheric variables are used to compute surface fluxes via MOST; typically, $Z_F = Z_1$ (Z_1 - FML height)
- ▶ When the FML is pushed towards the surface, we approach the limit of MOST ($Z_F \rightarrow z_{0m,h}$); decoupling the forcing level (Z_F) from the lowest model level (Z_1)
- ▶ Over heterogeneous surf., MOST breaks down locally. FML should be related to blending height, above which progn. variables no longer depend on local $z_{0m,h}$

GABLS1 case (101 levels)

$z_1 = 3.12$ m, $z_F = 3.12$ m



Initial approach for the safe lowering of the FML



Computation of turbulent fluxes:

$$\overline{(\psi'w')}_{UA} = -K_M \frac{\partial \overline{\psi}}{\partial z}; \quad \overline{(\phi'w')}_{UA} = -K_H \frac{\partial \overline{\phi}}{\partial z} + \text{TOMs}$$

$$K_M = C_K L_K \chi_3 \sqrt{e_k}; \quad K_H = C_3 C_K L_K \phi_3 \sqrt{e_k}$$

$$\overline{(\psi'w')}_s = C_M \sqrt{[\overline{u}^2(Z_F) + \overline{v}^2(Z_F)]} \left[\overline{\psi}(Z_F) - \overline{\psi}_s \right]$$

$$\overline{(\phi'w')}_s = C_H \sqrt{[\overline{u}^2(Z_F) + \overline{v}^2(Z_F)]} \left[\overline{\phi}(Z_F) - \overline{\phi}_s \right]$$

$$C_M = \frac{\kappa^2}{\ln^2 \left(1 + \frac{Z_F}{z_{0m}} \right)} F_M(Ri_g)$$

$$C_H = \frac{\kappa^2}{\ln \left(1 + \frac{Z_F}{z_{0h}} \right) \ln \left(1 + \frac{Z_F}{z_{0m}} \right)} F_H(Ri_g)$$

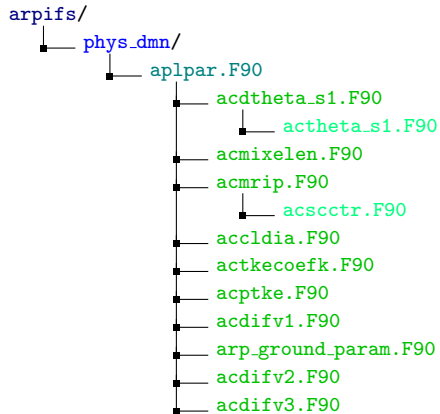
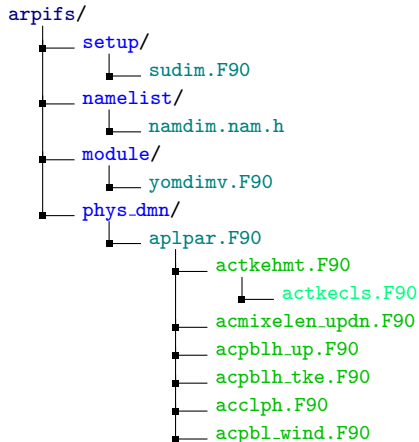
Screen-level interpolation:

Based on Z_F rather than Z_1

$\psi = u, v$; $\phi = s_L, q_t$; Z_F – forcing height

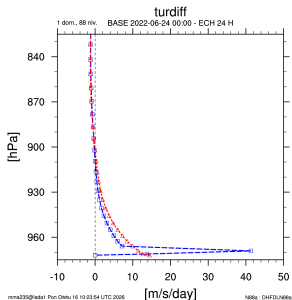
Initial approach for the safe lowering of the FML

- Currently implemented only in the ALADIN + ISBA framework within CY46T1_op3; activated via the namelist parameter NFLEVTUR

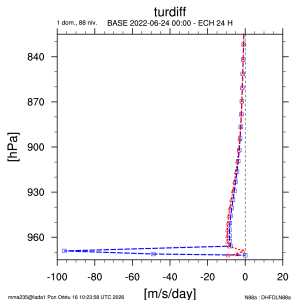


Initial approach for the safe lowering of the FML

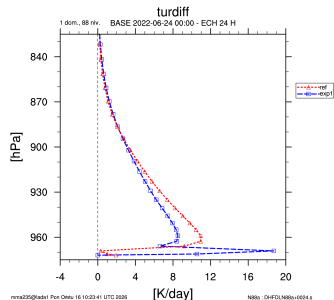
- ▶ The analysis using DDH budgets reveals spikes in tendencies due to turbulence at the interface between the constant-flux layer and the overlying layer employing the TKE formalism (new approach)
- ▶ Stronger near-surface wind than in KLEV=KLEVTUR experiment (old approach), with progressive distortion of wind and temperature fields aloft; adjustment of the concept is needed



zonal wind

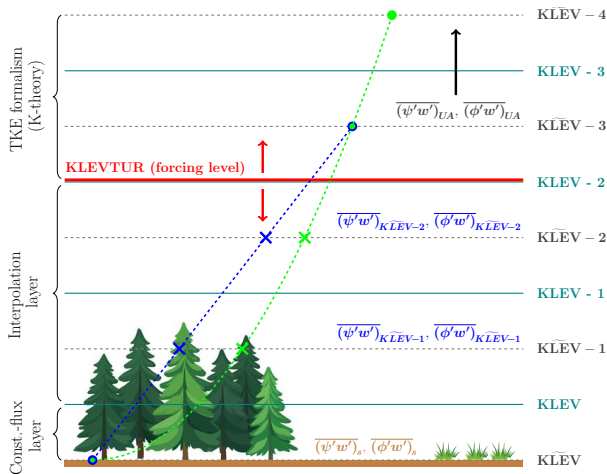


meridional wind



temperature

Revised approach for the safe lowering of the FML



Computation of turbulent fluxes:

$$(\overline{\psi'w'})_{UA} = -K_M \frac{\partial \overline{\psi}}{\partial z}; \quad (\overline{\phi'w'})_{UA} = -K_H \frac{\partial \overline{\phi}}{\partial z} + \text{TOMs}$$

$$K_M = C_K L_K \chi_3 \sqrt{e_k}; \quad K_H = C_3 C_K L_K \phi_3 \sqrt{e_k}$$

$$(\overline{\psi'w'})_s = C_M \sqrt{[\overline{u^2}(Z_F) + \overline{v^2}(Z_F)]} [\overline{\psi}(Z_F) - \overline{\psi}_s]$$

$$(\overline{\phi'w'})_s = C_H \sqrt{[\overline{u^2}(Z_F) + \overline{v^2}(Z_F)]} [\overline{\phi}(Z_F) - \overline{\phi}_s]$$

$$C_M = \frac{\kappa^2}{\ln^2 \left(1 + \frac{Z_F}{z_{0m}} \right)} F_M(Ri_g)$$

$$C_H = \frac{\kappa^2}{\ln \left(1 + \frac{Z_F}{z_{0h}} \right) \ln \left(1 + \frac{Z_F}{z_{0m}} \right)} F_H(Ri_g)$$

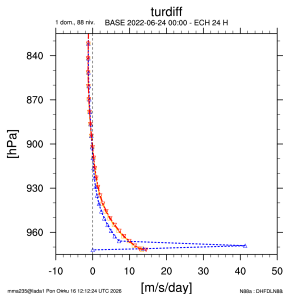
$$\psi = u, v; \quad \phi = s_L, q_t;$$

$$Z_F - \text{forcing height}$$

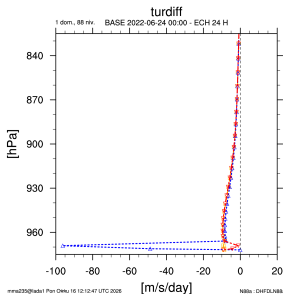
Fluxes $(\dots)_{\widetilde{KLEV-1}}$ and $(\dots)_{\widetilde{KLEV-2}}$: interpolation between $\widetilde{KLEV}$ and $\widetilde{KLEV-3}$ (and $\widetilde{KLEV-4}$)

Revised approach for the safe lowering of the FML

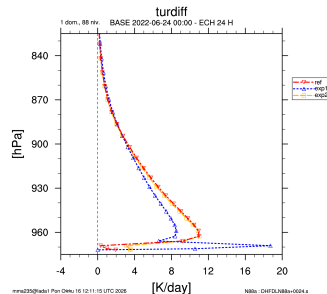
- ▶ In revised approach: (i) near equilibrium ($SP + BP \approx \epsilon$), the TKE scheme asymptotically converges to MOST (interp. layer effectively "invisible"); (ii) farther from equilibrium: controlled departure from MOST, ensuring smooth and physically consistent coupling with the TKE-based scheme.
- ▶ Removes spikes in tendency profile and closely reproduces KLEV=KLEVTUR exp., except near the surf.
- ▶ Adjustment is required for TKE and TTE diagnostics below KLEVTUR; affects their advection and diffusion



zonal wind



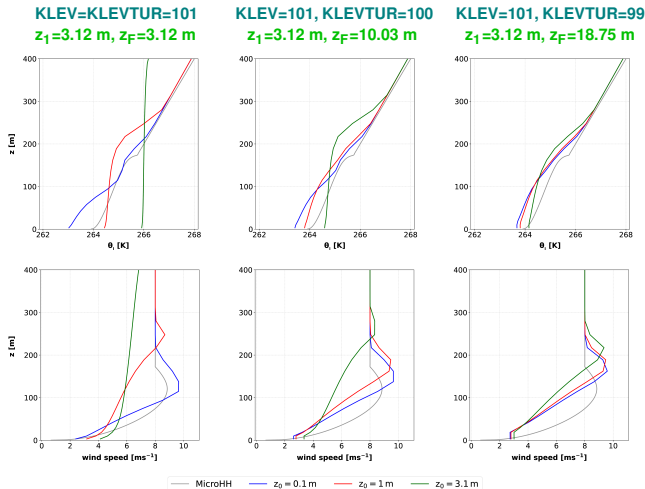
meridional wind



temperature

Revised approach for the safe lowering of the FML

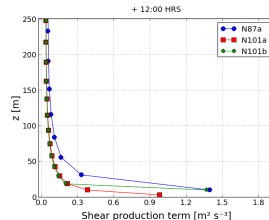
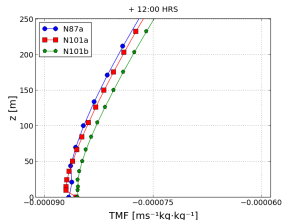
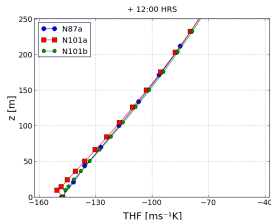
- ▶ The impact of revised approach and Z_F in the GABLS1 case (SABL)
- ▶ When $z_F \rightarrow z_0$:
 - (i) Old approach: turbulent mixing is too strong (flat θ_l and WSPD profiles)
 - (ii) New approach (revised): less sensitivity to errors in surf. databases and $z_{0m,h}$
- ▶ 3D model: strong impact of z_F on the near-surface WSPD profile (revised approach)



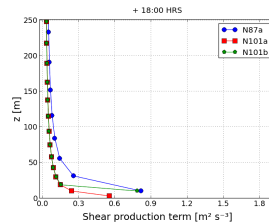
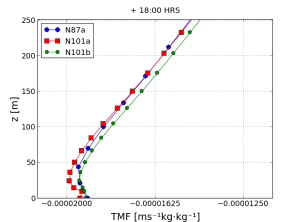
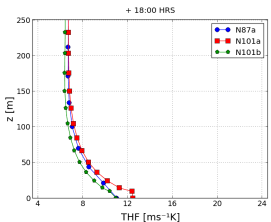
Revised approach for the safe lowering of the FML

- Domain-averaged turbulent fluxes of scalars and the shear term from 3D model (24 June 2022)

+ 12:00

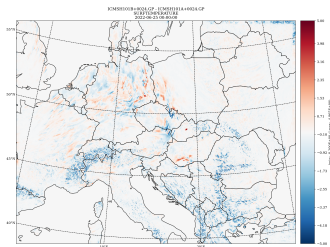


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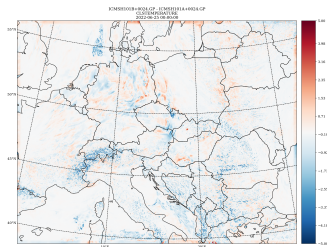


Revised approach for the safe lowering of the FML

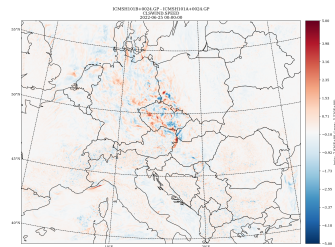
- ▶ Spatial differences in near-surface fields 24-h after the initialization (new approach - old approach)
- ▶ The statistical verification on winter and summer periods is ongoing:
 - (i) clear improvement in T2m, W10m and CLD over the 87-level reference; N101b and N101a comparable
 - (ii) grouping stations based on z_0 or z_F/z_0



surf. temperature



2-m temperature



10-m wind speed

- ▶ Old vs. new (revised) approach for a safe decrease of the FML:

aspect	old (KLEV = KLEVTUR)	new (KLEV < KLEVTUR)
MOST application	Always	Relaxed farther from equilibrium
Constant-flux layer	Strictly enforced	Relaxed farther from equilibrium (departure can be bounded)
Numerical stability	Problematic when $z_F \rightarrow z_0$	Enhanced
Consistency with the TKE scheme	Potential inconsistency near the surface	Enhanced due to smooth transition
Sensitivity to $z_{0m,h}$	High	Reduced
Suitable for heterogeneous gridbox	No	Partly

- ▶ Further steps: (i) code refinement/reorganization and more detailed validation, (ii) preparing IAL code contribution and (iii) implementation within the ALARO + SURFEX framework (relating z_F to blending height?)
- ▶ There is a related report at: https://www.rclace.eu/media/files/Physics/2025/MH_2024-2025P_KLEVTUR.pdf

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Thank you for your attention!



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