

Derivation of Structure Functions over the Copernicus Arctic Regional Reanalysis (CARRA-2) Region

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Introduction: Data Assimilation

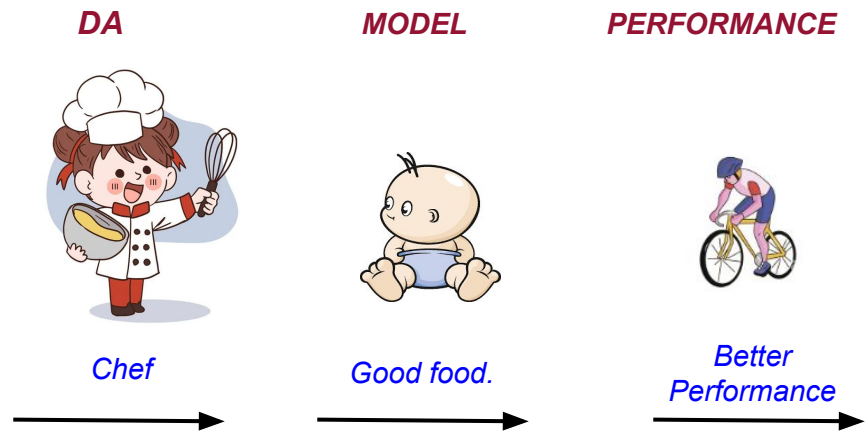
Data Assimilation is the combination of information from a model and observations to produce a best estimate of the state of the atmosphere (the analysis).

Fundamental issues:

- *Problem is under-determined: not enough observations to define the state.*
- *Forecast error covariances cannot be determined from observations.*
- *Large scale problem.*
- *Nonlinear system.*

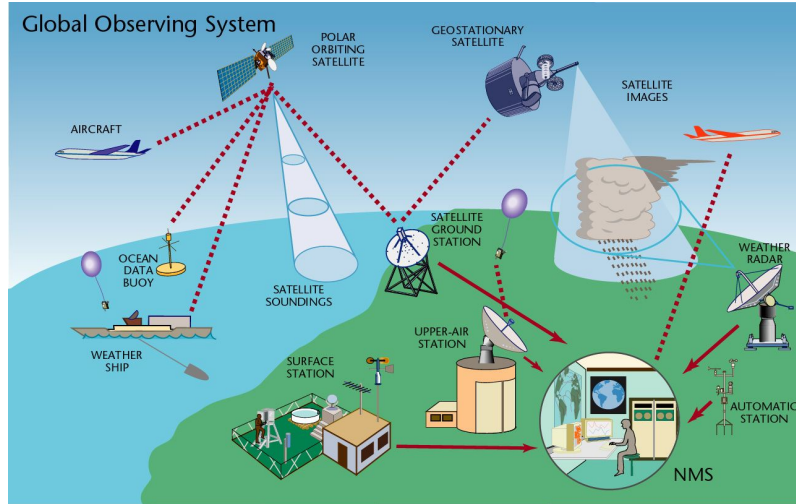
Methods:

- **Variational (3D/4D-VAR)**
- *Extended Kalman Filter (EKF)*
- *Ensemble Kalman Filter (EnKF)*
- *Hybrid Method (3D/4D-VAR + EnKF)*



Introduction: Observation

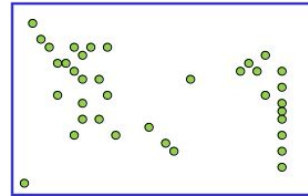
We are far from using all the observations.



@ ECMWF

- *Observation quality dependent.*
- *Observing system dependent.*
- *NWP model resolution dependent.*
- *Assimilation method dependent.*

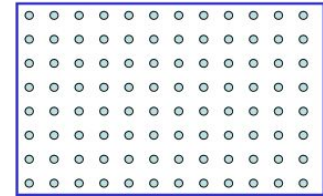
Observation Irregularity



Analysis

X

Regular Grid Point



Good observations only cover part of the model domain which provide incomplete model state at given locations. In addition, many observations are not NWP model variables.

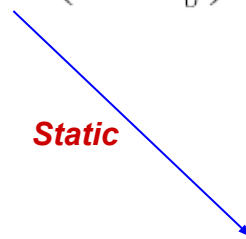
Quality Control:

- *Bad reporting practice check*
- *Probability Gross Error check (against some limits)*
- *Background check (short-range forecasts)*
- *Observation Thinning*
- *Analysis check: Var-QC*

Introduction: 3D-Variational DA

$$J(\mathbf{x}) = \frac{1}{2}(\mathbf{x} - \mathbf{x}_b)^T \mathbf{B}^{-1}(\mathbf{x} - \mathbf{x}_b) + \frac{1}{2}(\mathbf{y} - \mathbf{h}(\mathbf{x}))^T \mathbf{R}^{-1}(\mathbf{y} - \mathbf{h}(\mathbf{x}))$$

Static


$$\mathbf{B} = \begin{pmatrix} \langle \boldsymbol{\varepsilon}_1^2 \rangle & \langle \boldsymbol{\varepsilon}_1 \boldsymbol{\varepsilon}_2 \rangle & \dots \\ \langle \boldsymbol{\varepsilon}_2 \boldsymbol{\varepsilon}_3 \rangle & \langle \boldsymbol{\varepsilon}_2^2 \rangle & \dots \\ \vdots & \vdots & \ddots \end{pmatrix}$$

Potential Problem:

Relies heavily on correct B matrix.

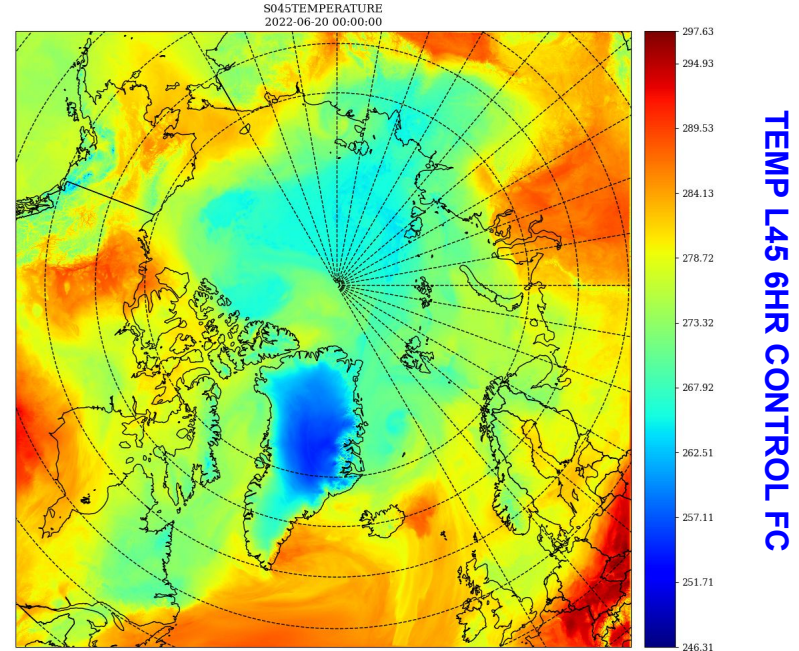
Typically no error estimate.

Copernicus Arctic Regional Reanalysis (CARRA-2)



Derivation and the importance of background error statistics (B-matrix) over the Copernicus Arctic Regional Reanalysis Second Generation (CARRA2) region.

CARRA2 is an reanalysis product that extends to a larger area (spatial resolution 2.5 km and 2880 x 2880 grid points) to provide pan-Arctic coverage.



Horizontal Resolution: **2.5 km**,
Grid Points: **2880x2880**
Vertical levels : **65**

Introduction: FESTAT



The background error statistics (BGE) also referred as a Structure Functions, are produced through the standalone FESTAT (Forecast Error Statistics) method.

The control variables encompass vorticity, divergence, specific humidity, surface pressure, and temperature.

$$VDF(\delta x) = \begin{pmatrix} \delta u \\ \delta v \\ \delta T \\ \delta q \\ \delta \ln P_s \end{pmatrix}$$

- F**: Horizontal 2-dim Fourier transformation from physical grid point space to spectral space.
- D**: Balance operator or statistical de-correlation operator.
- V**: Vertical transform utilizing the eigen-vectors of vertical covariance matrices.

The FESTAT manages multiple tasks related to the error statistics, including (1) converting variables from gridpoint space to spectral point space, (2) computing the balance operator, (3) generating horizontal variance density spectra for control variables, and (4) determining vertical correlations for the control variables.

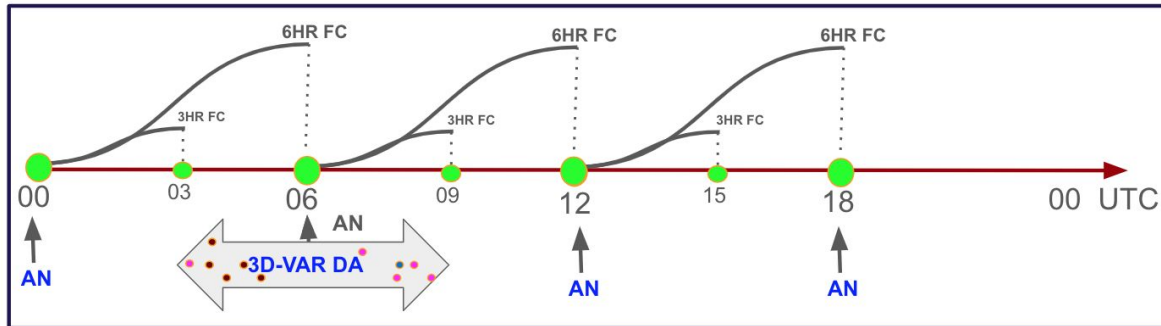
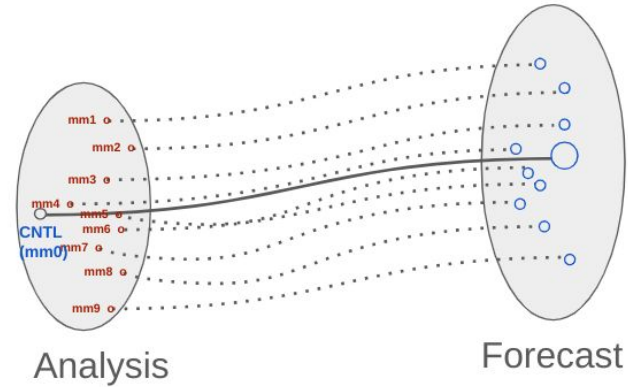
HarmonieEPS Configuration:

SMHI

BRAND:

B-matrix RANdOm (BRAND) perturbations are generated as Gaussian ($N(0,1)$) random numbers in the entire control vector space and are projected to the physical space of the model state applying the square-root of background error covariance.

The covariance estimator is based on circular differences between 10-members.



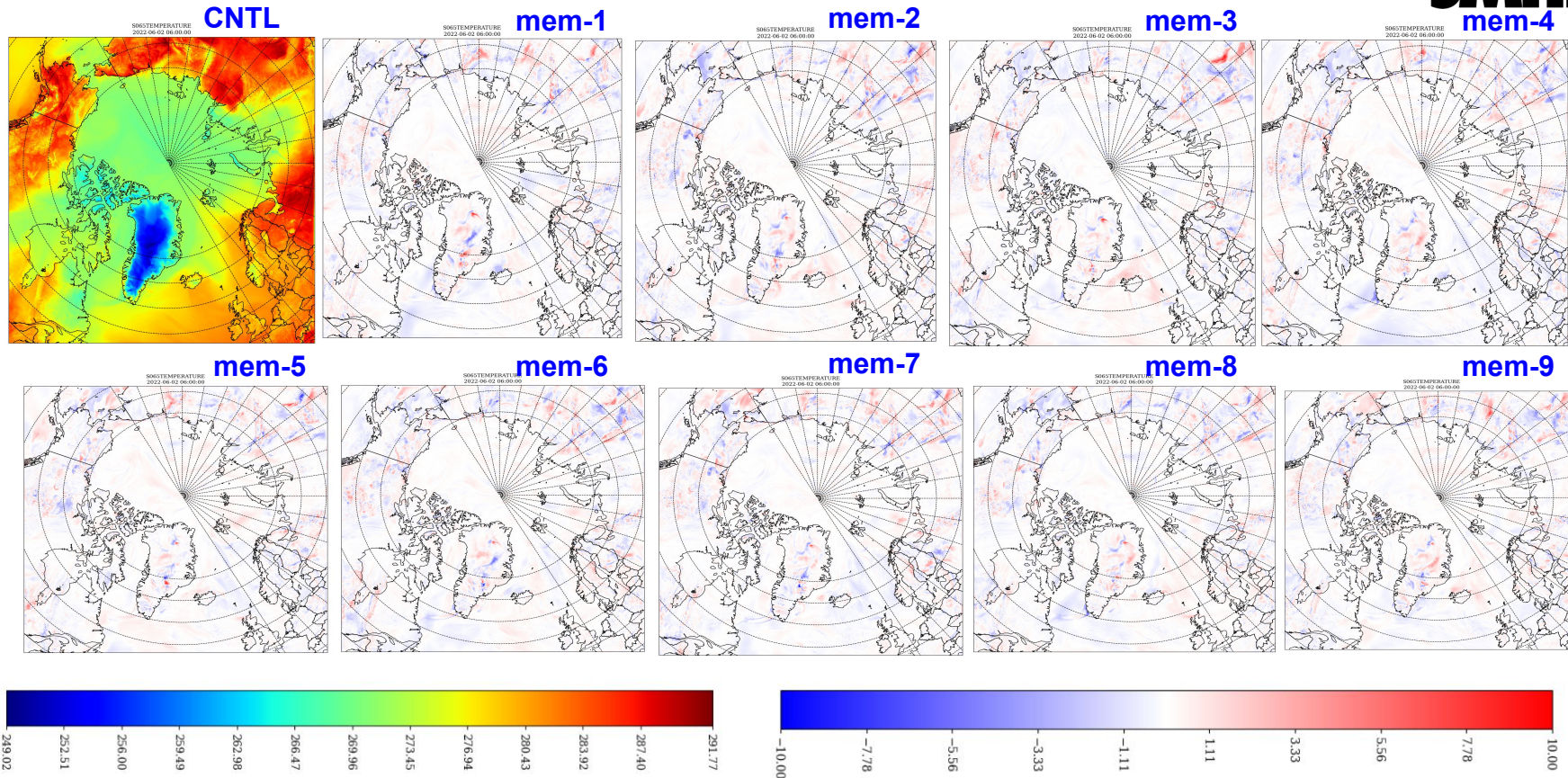
Ensemble Prediction System (EPS):

9-member (mm1–mm9) and a control, mm0.

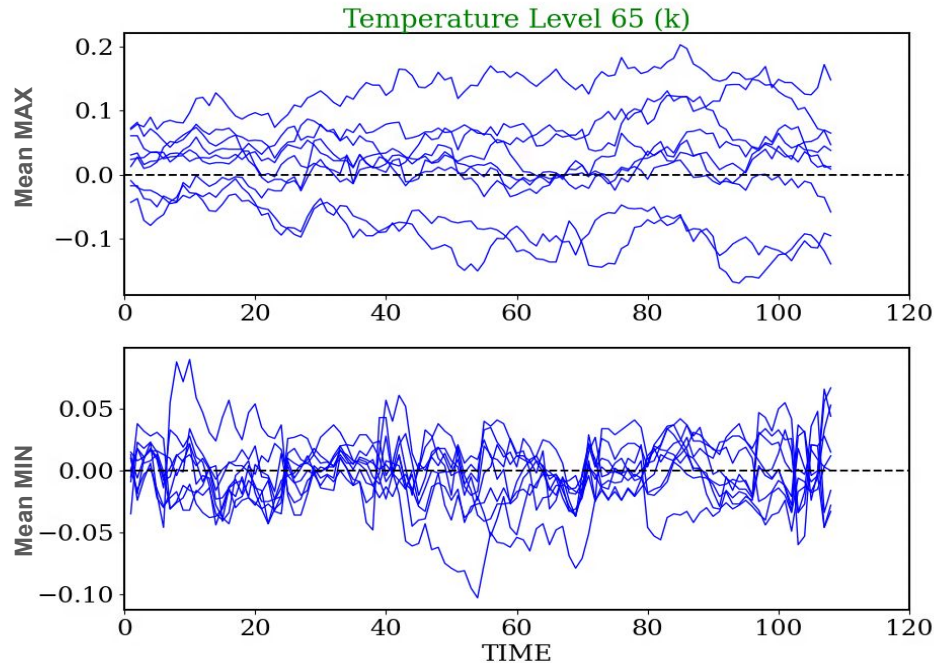
IC/BCs:

ERA5 EDA 10-ensemble members.

TEMPERATURE at LEVEL 65 (in Kelvin, 6HR FC)



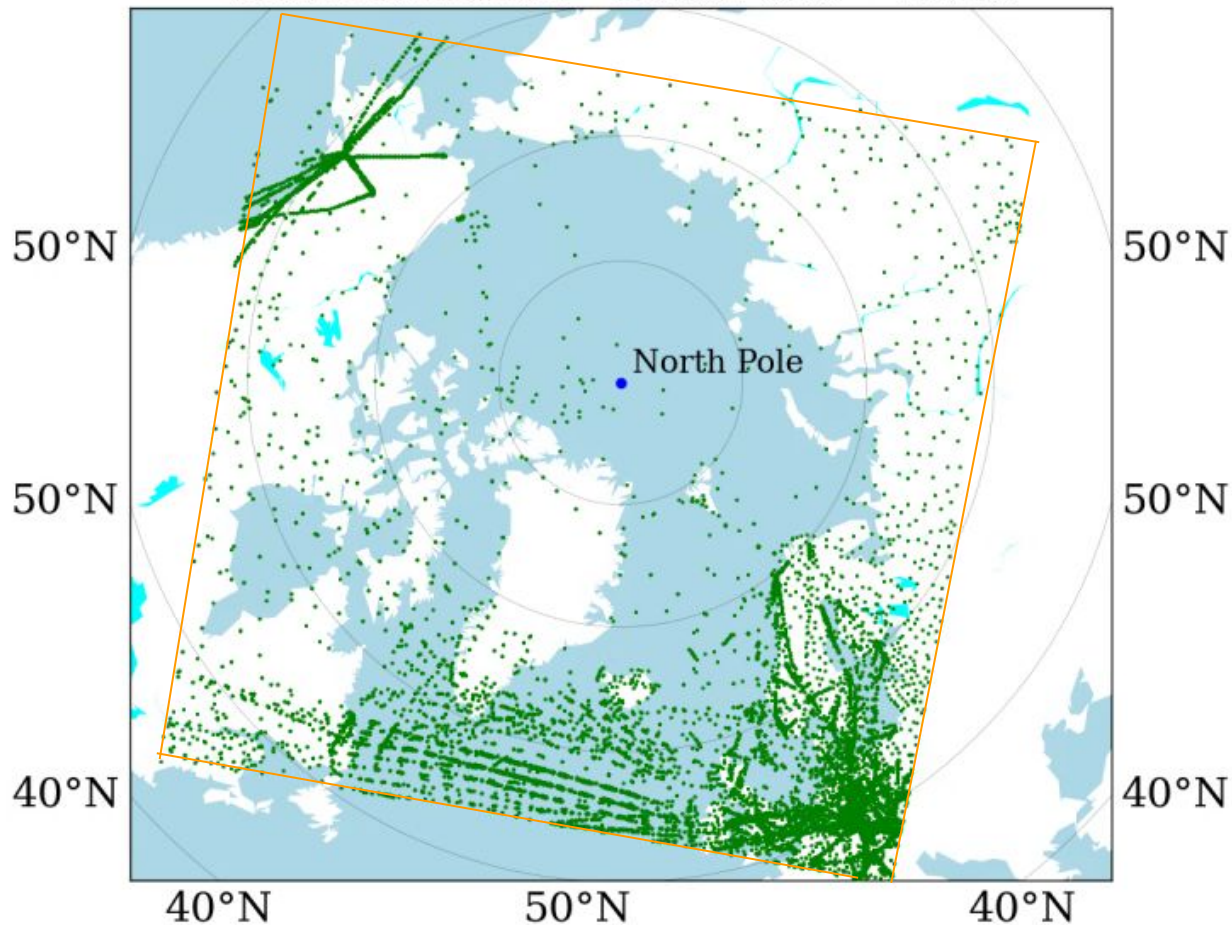
TEMPERATURE at LEVEL 65 (in Kelvin)



Time series of mean maximum and mean minimum temperature difference between control and each ensemble member (1-9) from 1 to 28 June 2022 and for each assimilation cycle (00, 06 12 and 18 UTC).

```
CARRA2_CY46
├── InitRun ▲ ⚠
│   └── MakeCycleInput
│       └── Date
│           YMD=... 20220215
│           ( InitRun == complete )
│               └── Hour
│                   HH=... 18 ...
│                   (( ( ../Date:YMD <= 20220215 )
│                       └── Cycle
│                           ├── Mbr000
│                           ├── Mbr001
│                           ├── Mbr002
│                           ├── Mbr003
│                           ├── Mbr004
│                           ├── Mbr005
│                           ├── Mbr006
│                           ├── Mbr007
│                           ├── Mbr008
│                           └── Mbr009
│                           ├── CollectLogs ▲
│                           └── LogProgress ▲
│                               └── Postprocessing
```

CONVENTIONAL TOTAL OBS = 45746



Data Assimilation

3D-VAR system

Assim OBS: (20220602 at 00-UTC)

SYNOP

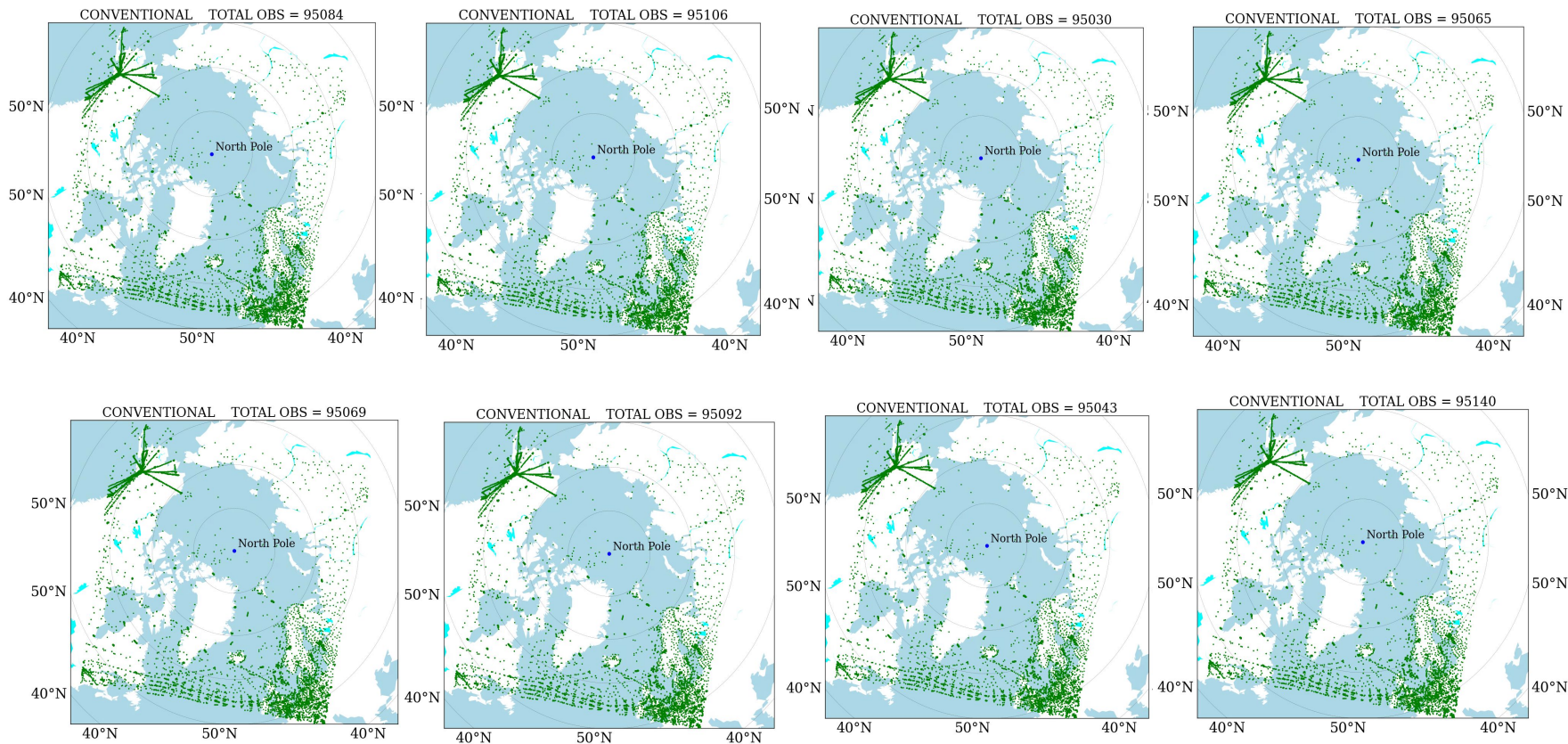
AIRCRF

BUOY

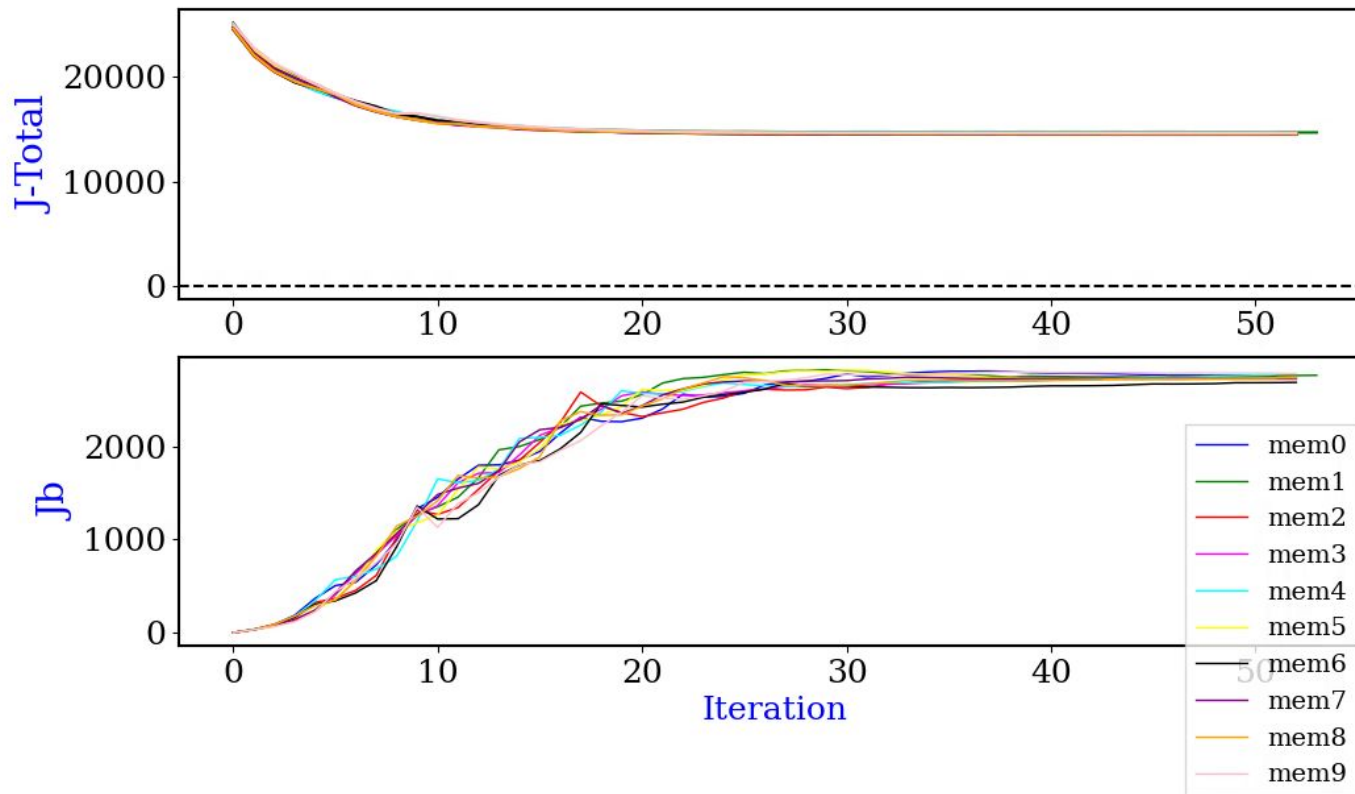
TEMP

PILOT

Assimilated Observation (20220602 at 00-UTC)



Cost Function Valid on 20230615 at 06 UTC



B-Matrix:

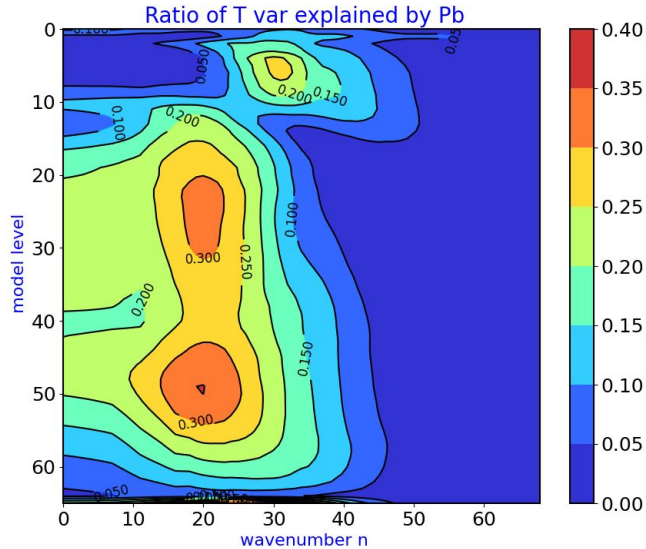


Cases	Valid from	Season	Forecast hour	No. of files	LUNBC	Validated
B1	20230101 to 20230215	Winter	6 HR	999	FALSE	20140701 to 20140715
B2	20230601 to 20230715	Summer	6 HR	999	FALSE	20140701 to 20140715
B3	20230601 to 20230715	Summer	12 HR	999	FALSE	20140701 to 20140715
B4	20230601 to 20230715	Summer	6 HR	999	TRUE	20140701 to 20140715

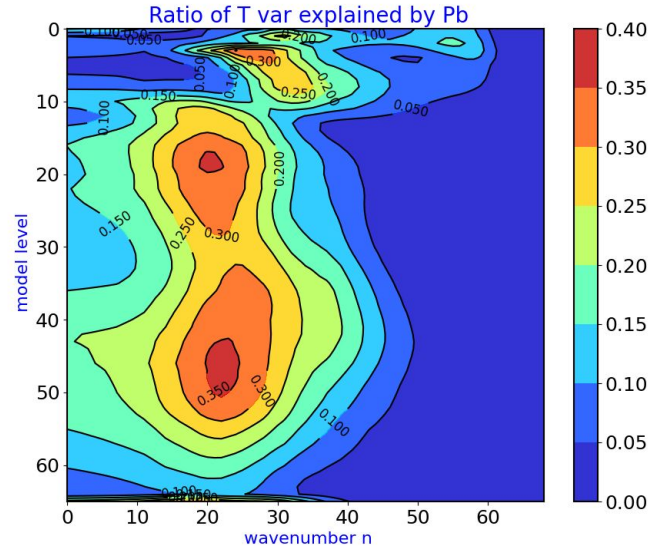
***LUNBC: Upper Nested Boundary Conditions
(Switch : TRUE/ FALSE)***

B-Matrix:

WINTER (B1)

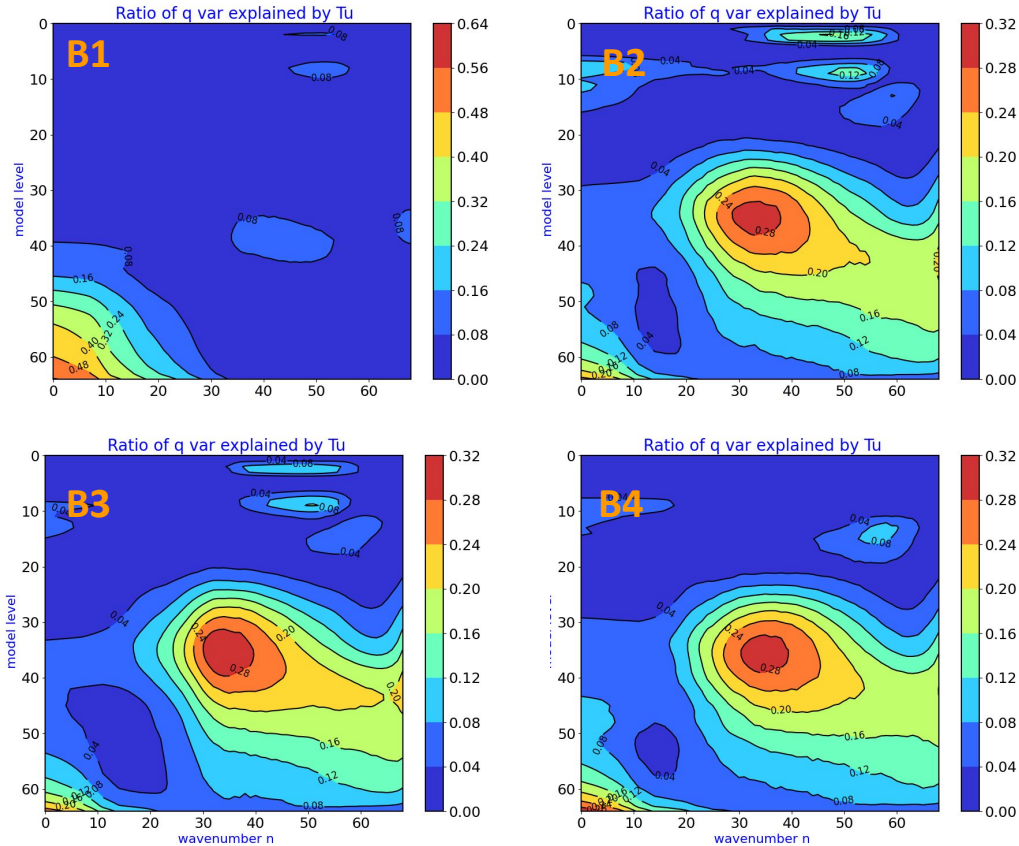


SUMMER (B2)



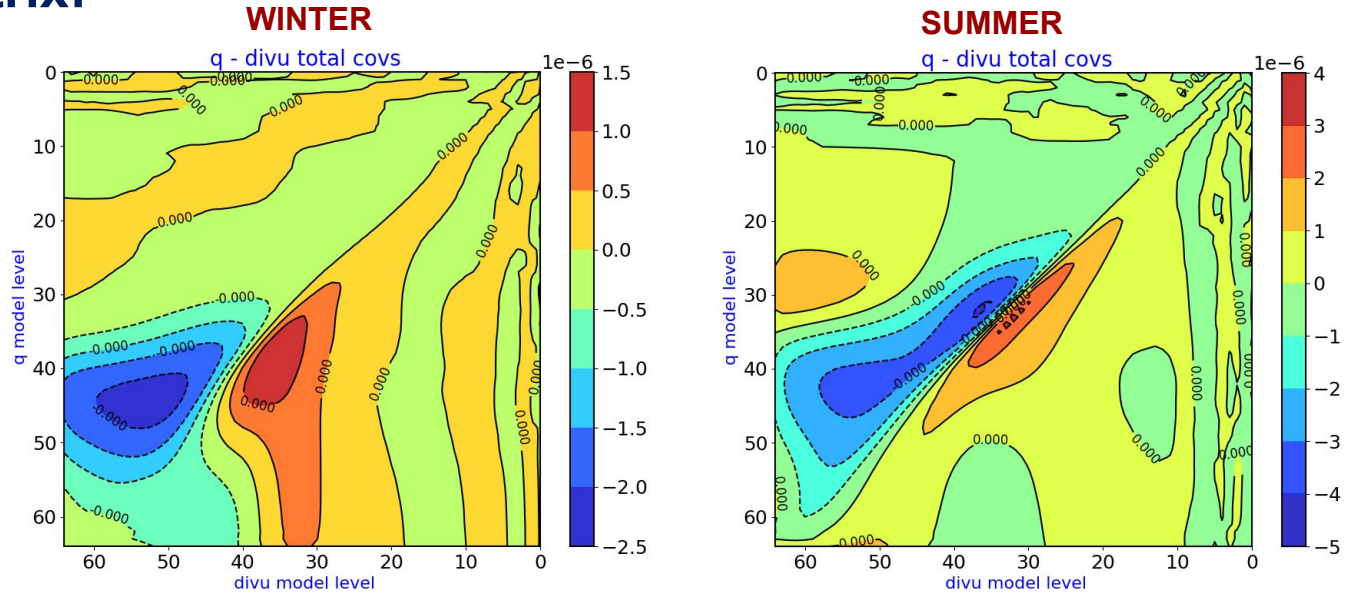
Percentage of the variance of temperature that is explained by balanced geopotential as a function of height and wave number.

B-Matrix:



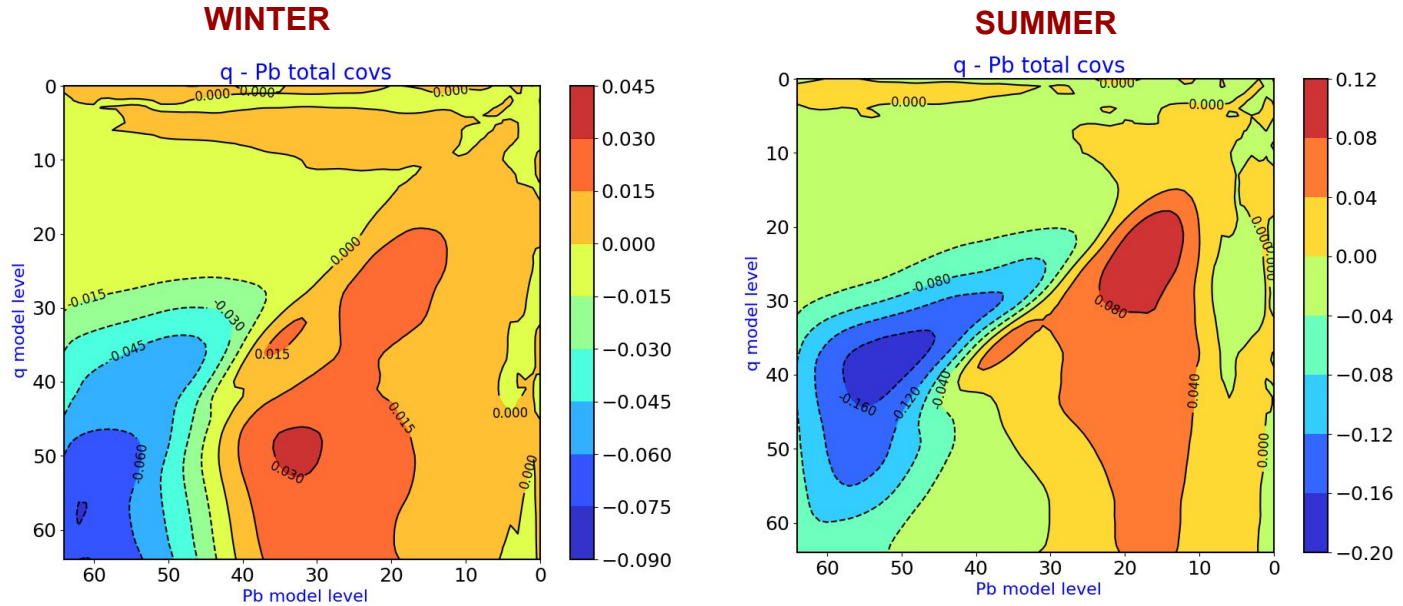
Percentage of the variance of specific humidity that is explained by Tu as a function of height and wave number.

B-Matrix:



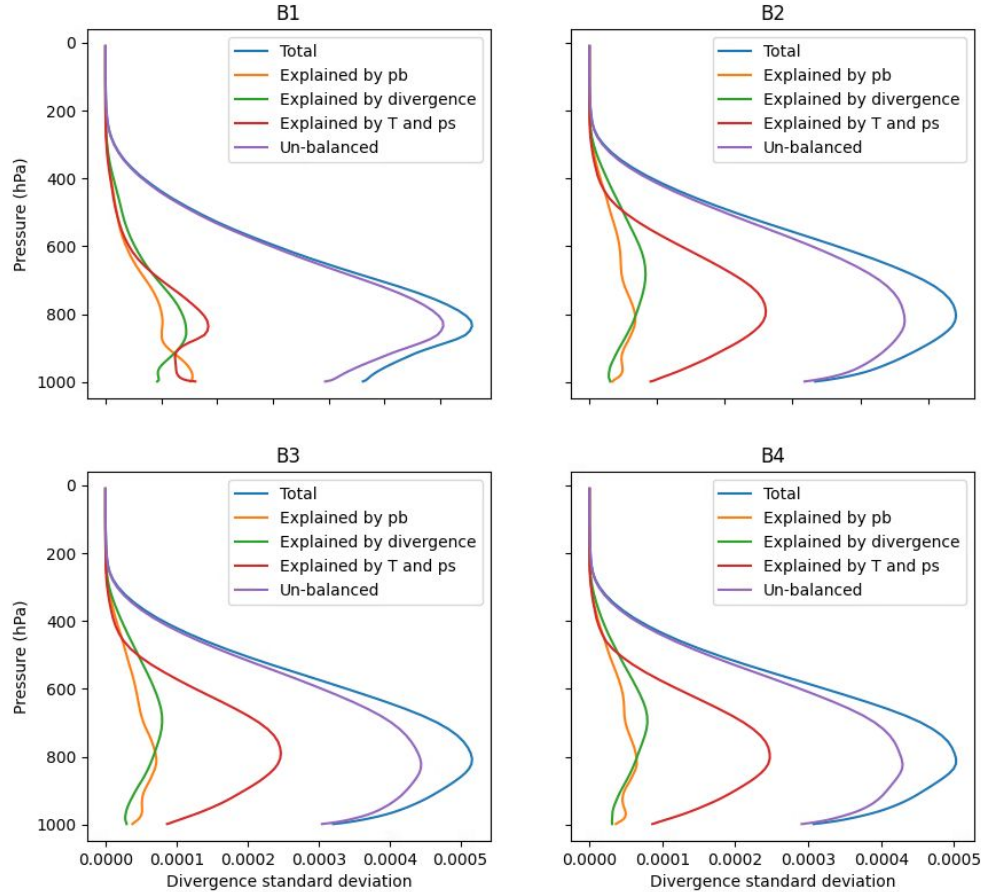
Average vertical cross-covariance matrix between specific humidity and unbalanced divergence ($\text{kg kg}^{-1} \text{s}^{-1}$).

B-Matrix:



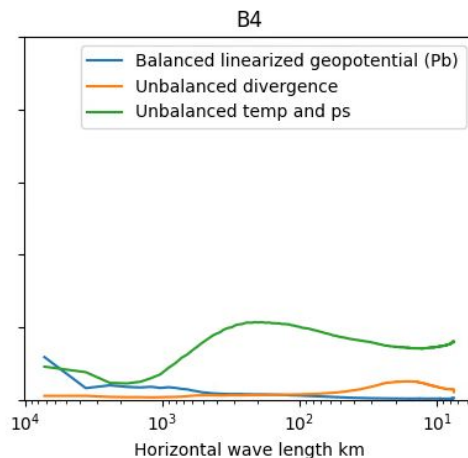
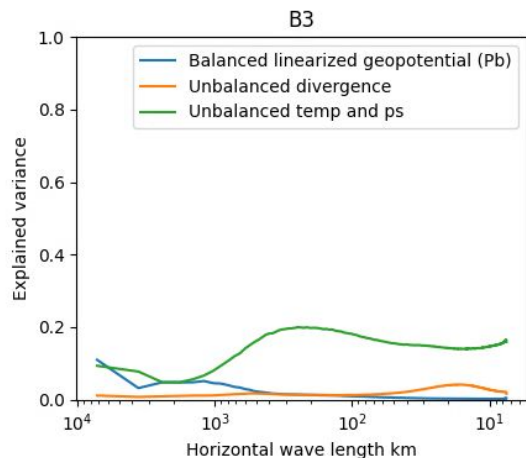
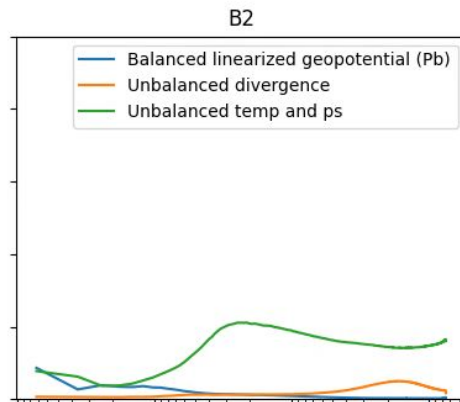
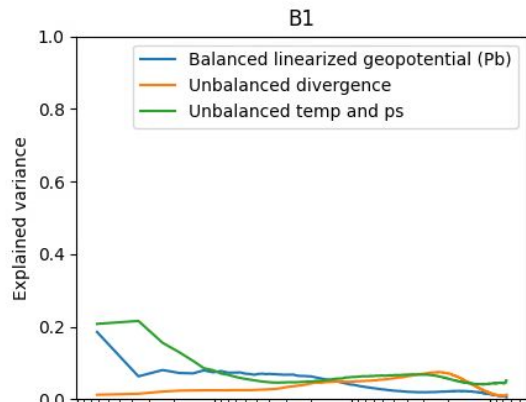
Average vertical cross-covariance matrix between specific humidity and vorticity-balanced geopotential ($\text{kg kg}^{-1} \text{J}$).

B-Matrix:



Background error standard deviations for humidity.

B-Matrix:

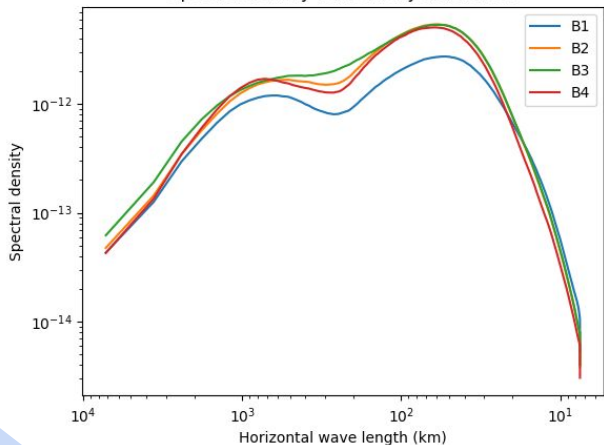


Percentages of humidity background error variances explained by vorticity, unbalanced divergence and unbalanced temperature and surface pressure as a function of horizontal wavelength.

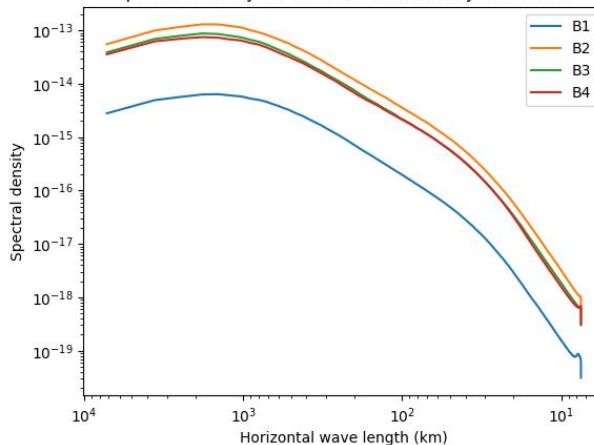
B-Matrix:



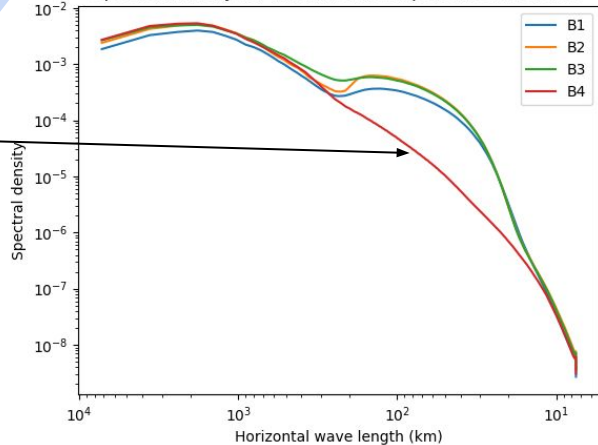
Spectral density for vorticity at level 10



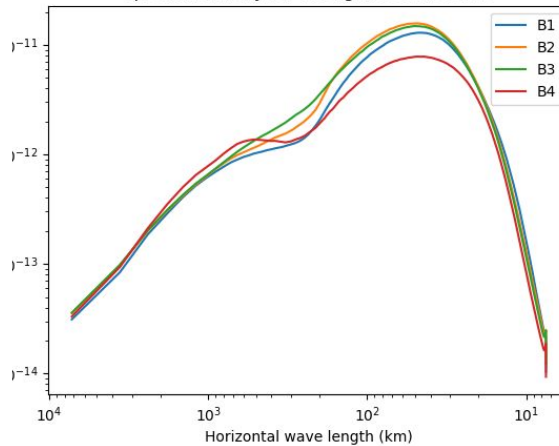
Spectral density for unbalanced humidity at level 10



Spectral density for unbalanced temperature at level 10



Spectral density for divergence at level 10



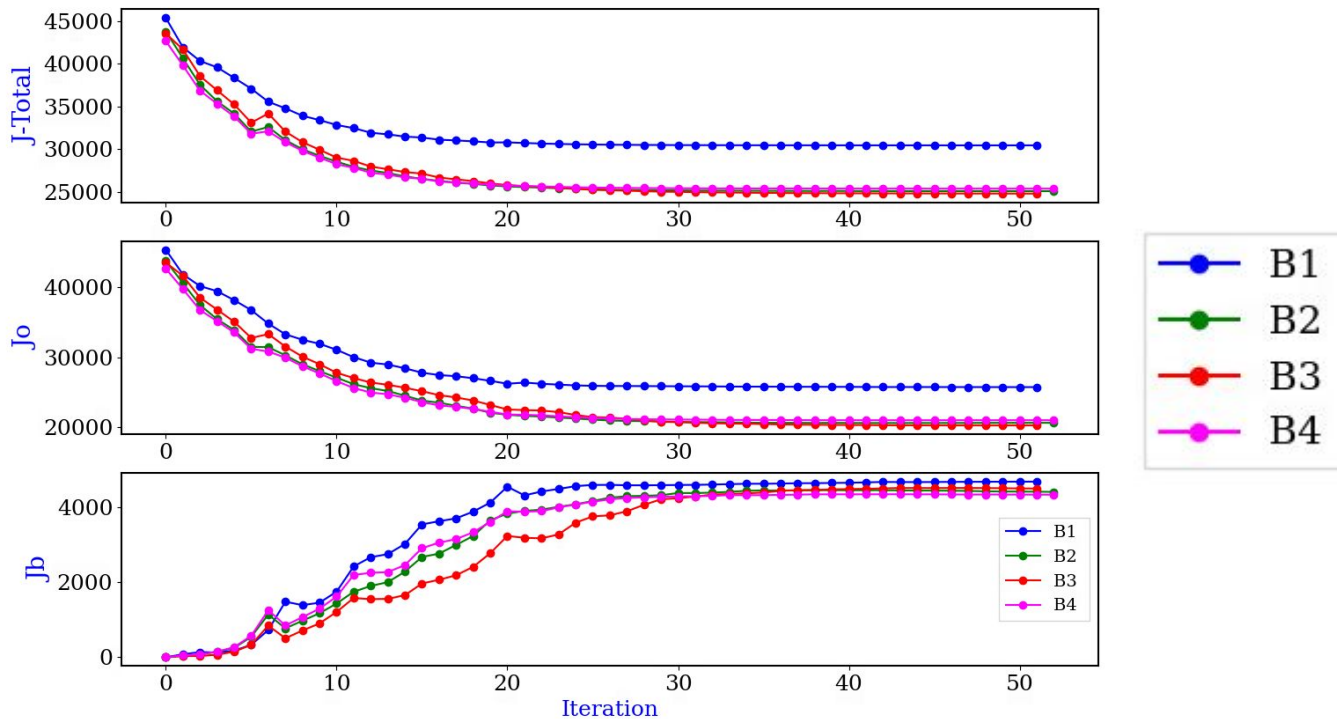
B4, upper nested boundary conditions (LUNBC=True)

Level 10 spectral density at different horizontal wavelength (km).

Validation:



Cost Function Valid on 20150716 at 18 UTC



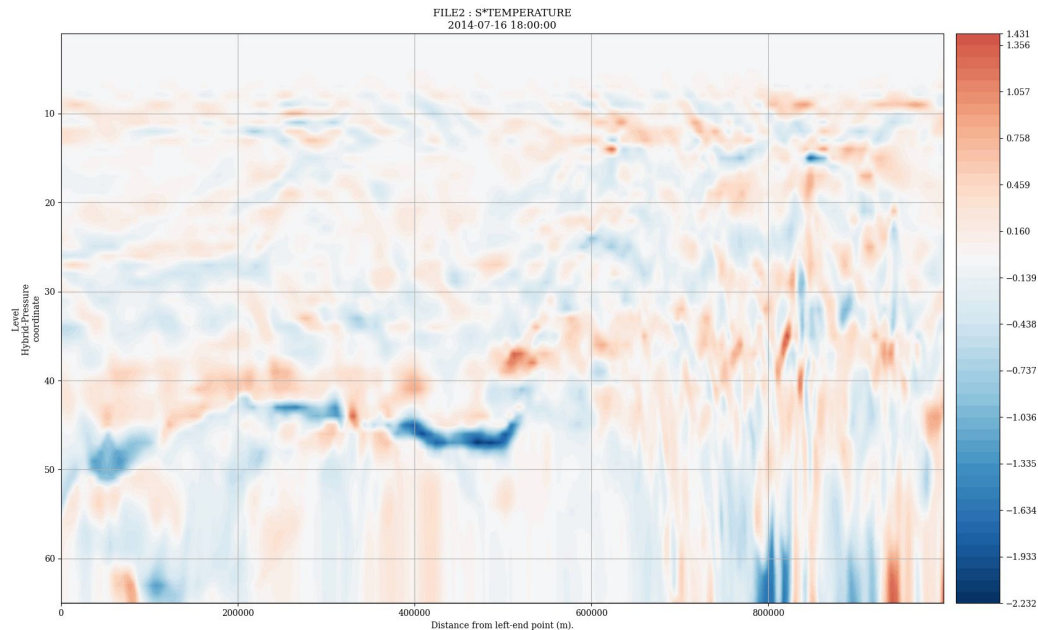
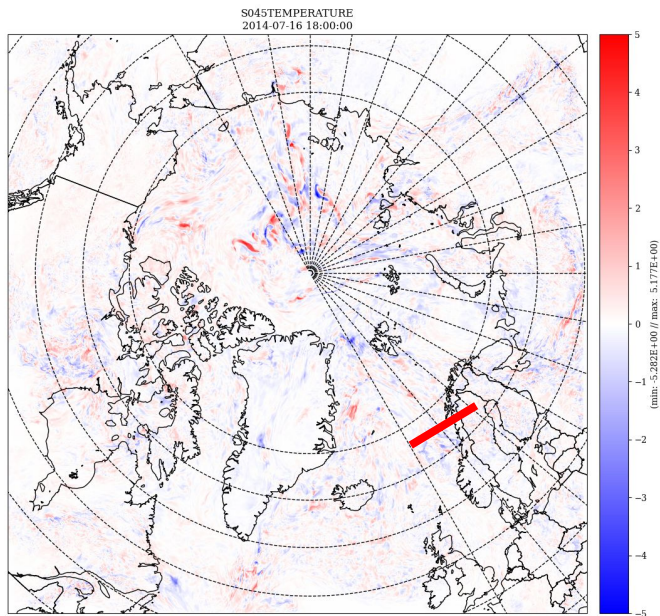
Validation:

Validate on 20150716 at 18 UTC



Temperature DIFF L45
(B2 - B4) in K

Temperature Cross-section DIFF
(B2 - B4) in K
- (0.0E,64.5N) and (21.5E, 67.0N)

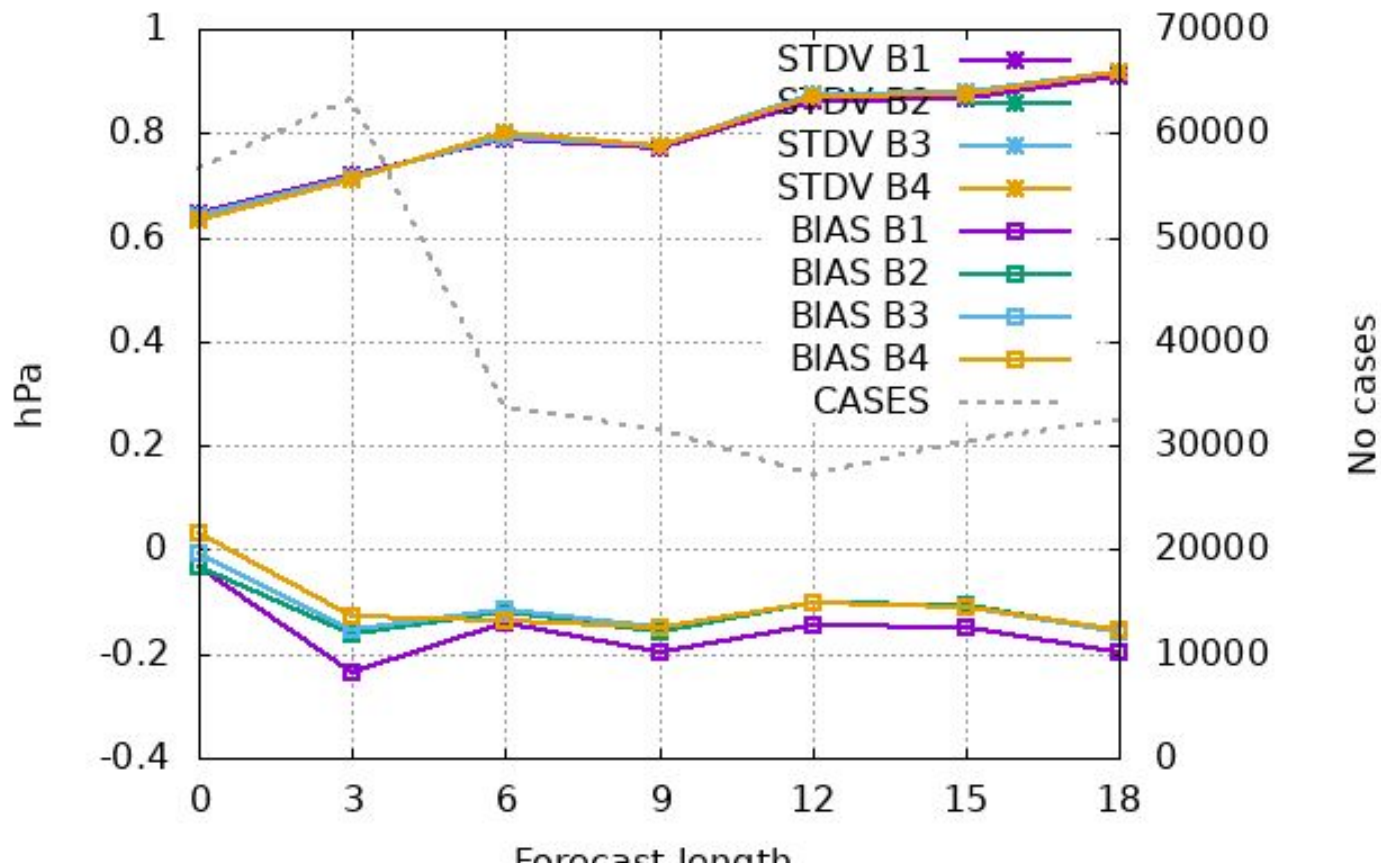


B2 : LUNBC=FALSE

B4: LUNBC=TRUE

Validate on 201507

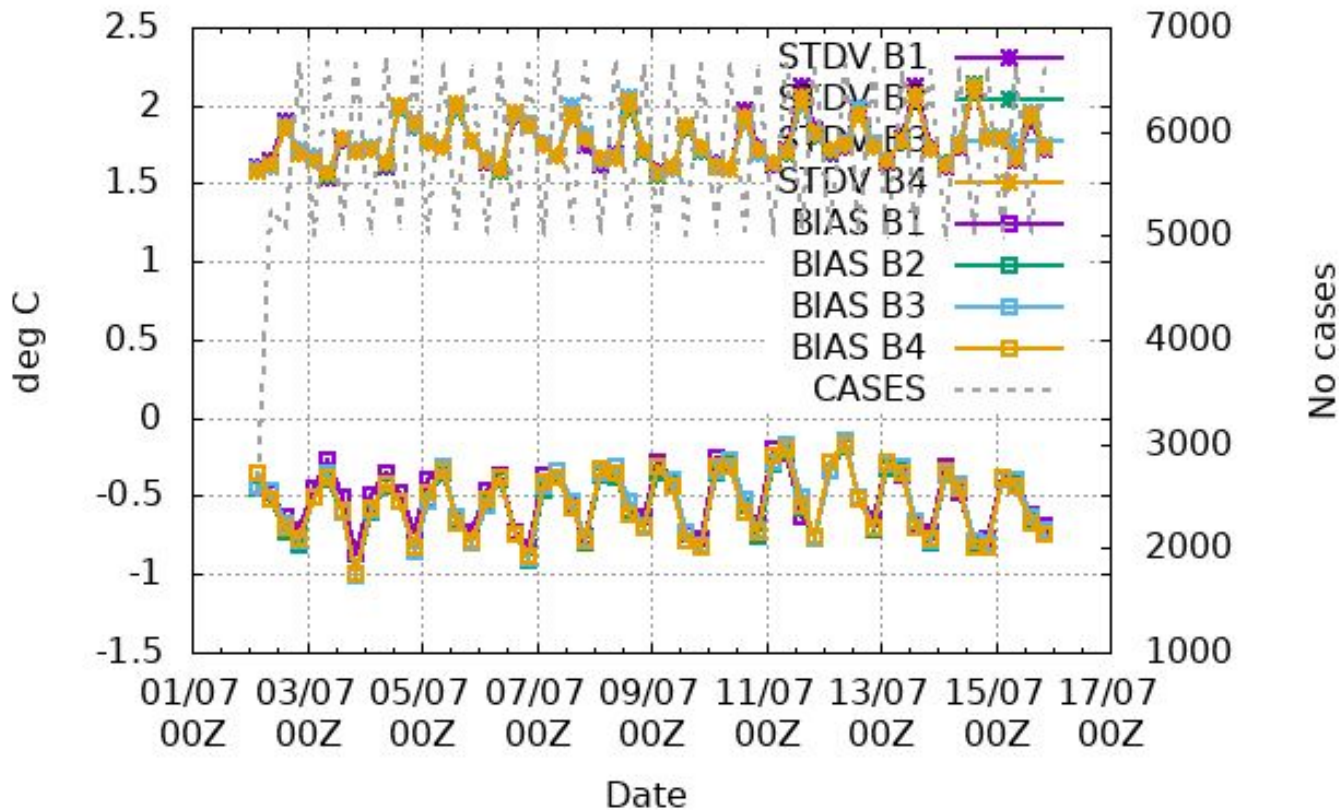
Selection: ALL using 1226 stations
Mslp Period: 20140702-20140715
Hours: 00,06,12,18



Validate on 201507



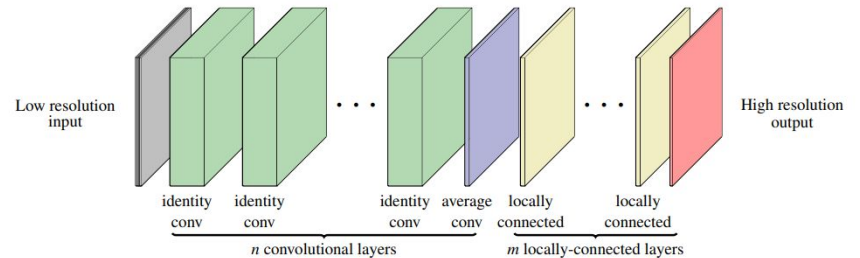
T2m
Selection: ALL 1444 stations
Used 00,06,12,18 + 00 03 06 09 12 15 18
Averaging window: 6h



Next:

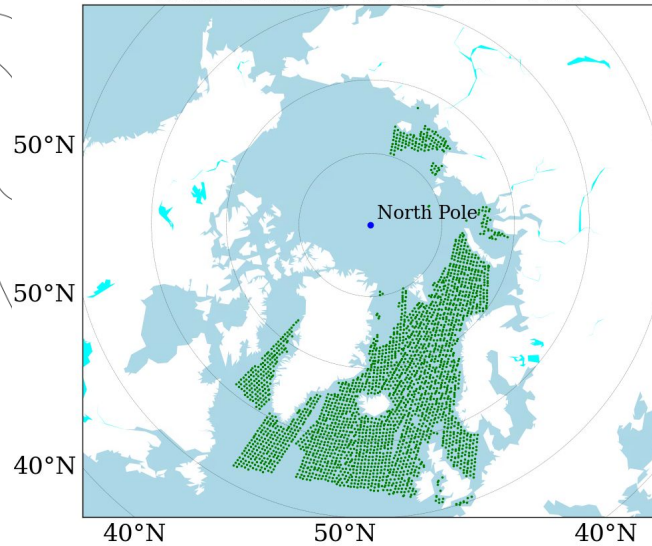
1. The results are presently being integrated into a draft of the paper.
2. An Approach Leveraging Machine Learning. Uncertainty Estimation in Ensembles Across the CARRA Domain:

Super-Resolution Convolutional Neural Networks (SRCNN):

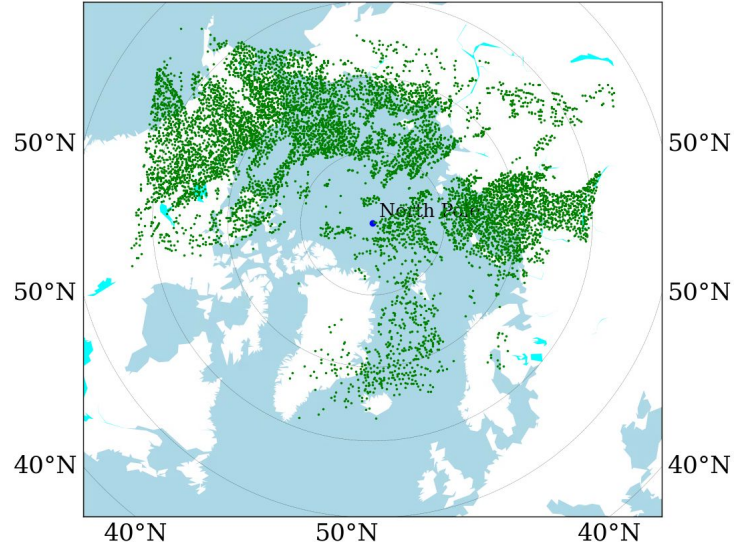


3. Variational Quality control (VAR-QC) over CARRA2.

*Scatterometers, retrieve wind from
backscatter*



*AMVs, retrieve wind Cloud and
Moisture*



Thank You..