

**Impacts of changes in:**  
**(1) the conservation of “pseudo-enthalpy” (Arpege/Alaro)**  
**(2) the turbulent mixing length (Arpege/Arome)**

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By **Pascal Marquet** (Météo-France / DESR / CNRM / GMAP)  
with **Yves Bouteloup, Eric Bazile, Yann Seity,**  
and **Jean-François Gueremy**

ACCORD Workshop, Toulouse (15th April, 2021)



# Outline

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**1) The conservation of “Pseudo-enthalpy”: a need to set “ZDEC=0” in CPUTQY**

2) Impacts of “ZDEC=0” in CPUTQY

3) A new way to compute the mixing length “L” in “ACBL89” and “BL89”

4) Impacts of the new “L” in “ACBL89” + “BL89”

5) Conclusions

Equations for: (1) **kinetic** energy, (2) **potential** energy, and (3) “**Cp T**”

(1): $K = (u^2 + v^2)/2$	$\frac{dK}{dt} = \boxed{-\vec{v} \cdot \vec{\nabla}_\eta(\phi)} - \frac{RT}{p} \vec{v} \cdot \vec{\nabla}_\eta(p) - \boxed{D_K}$ $\frac{d\phi}{dt} = \frac{\partial\phi}{\partial t}\Big _\eta + \vec{v} \cdot \vec{\nabla}_\eta(\phi) + \dot{\eta} \frac{\partial\phi}{\partial\eta}$ $\frac{d(c_p T)}{dt} = \frac{1}{\rho} \frac{\partial p}{\partial t}\Big _\eta + \frac{RT}{p} \vec{v} \cdot \vec{\nabla}_\eta(p) - \dot{\eta} \frac{\partial\phi}{\partial\eta} + \boxed{G_{cpT}}$	
(2): $\phi = g z$		<span style="color: orange;">Changes in <math>K</math></span>
(3): $c_p T$		<span style="color: orange;">Changes in <math>c_p T</math></span>

$c_p = q_d c_{pd} + q_v c_{pv} + q_l c_l + q_i c_i$

(1) + (2) + (3):

“ $c_p T + K + \phi$ ”

$$\frac{d(c_p T + K + \phi)}{dt} = \frac{1}{\rho} \frac{\partial p}{\partial t}\Big|_\eta + \frac{\partial\phi}{\partial t}\Big|_\eta + \boxed{G_{cpT}} - \boxed{D_K}$$

The “pseudo-enthalpy”

# Equations for the “pseudo-enthalpy”: physical tendencies?

(neglected or =0...)

“ $c_p T + K + \phi$ ”  
“pseudo-enthalpy”

$$\frac{d(c_p T + K + \phi)}{dt} = \frac{1}{\rho} \frac{\partial p}{\partial t} \Big|_{\eta} + \frac{\partial \phi}{\partial t} \Big|_{\eta} + G_{cpT} - D_K$$

Changes in  $c_p T$

Changes in  $K$

$G_{cpT}$

$D_K$

(neglected)

$$\frac{\partial u}{\partial t} \Big|_{\text{phys}} \equiv \text{PTENDU} \approx \frac{\Delta u}{\Delta t}$$

$$\frac{\partial v}{\partial t} \Big|_{\text{phys}} \equiv \text{PTENDV} \approx \frac{\Delta v}{\Delta t}$$

$$\frac{\partial(c_p T + K (+ \phi?))}{\partial t} \Big|_{\text{phys}} \equiv \text{PTENDH} \approx \frac{\Delta(c_p T + K)}{\Delta t}$$

Question: is **PTENDH** = changes in  $c_p T + K$  ?

## Equations for the “pseudo-enthalpy”: **physical tendencies?**

Changes in  $(u,v)$  and thus  $K$

NO: changes in  $c_p T$  alone in the code!

In CPUTQY:

$$u_{(+)} = u_{(-)} + \text{PTENDU} \times \Delta t$$

$$v_{(+)} = v_{(-)} + \text{PTENDV} \times \Delta t$$

$$c_{p(+)} T_{(+)} = c_{p(-)} T_{(-)} + \text{PTENDH} \times \Delta t - \text{ZDEC} \times \Delta t$$

$$\frac{\Delta(c_p T + K)}{\Delta t} \approx \text{PTENDH}$$

“ZDEC” = a term added in CPUTQY to keep  $c_p T + K$  constant locally?

... for the Gravity Wave Drag for instance,  
 where changes in  $(u,v)$ , and thus  $K$ , but with **PTENDH=0**,  
 and changes in K implies local heating or cooling in CPUTQY!

## Equations for the “pseudo-enthalpy”: physical tendencies?

Changes in  $(u,v)$  and thus  $K$

NO: changes in  $c_p T$  alone in the code!

In CPUTQY:

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$$v_{(+)} = v_{(-)} + \text{PTENDV} \times \Delta t$$

$$c_{p(+)} T_{(+)} = c_{p(-)} T_{(-)} + \text{PTENDH} \times \Delta t - \text{ZDEC} \times \Delta t$$

$$\frac{\Delta(c_p T + K)}{\Delta t} \approx \text{PTENDH}$$

... the same for GWD, convection, turbulence, ... : a need to set **ZDEC=0**?

- a too strong constraint revealed by Yves Bouteloup (test of Tiedtke scheme)
- **ZDEC** was just for “debug” mode (dixit Michel Déqué, who told with JFG...)
- even if local conservation  $\Rightarrow$  global one / the reverse must not be applied!
- nothing similar to ZDEC in IFS or other models...

# Outline

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1) The conservation of “Pseudo-enthalpy”: a need to set “ZDEC=0” in CPUTQY

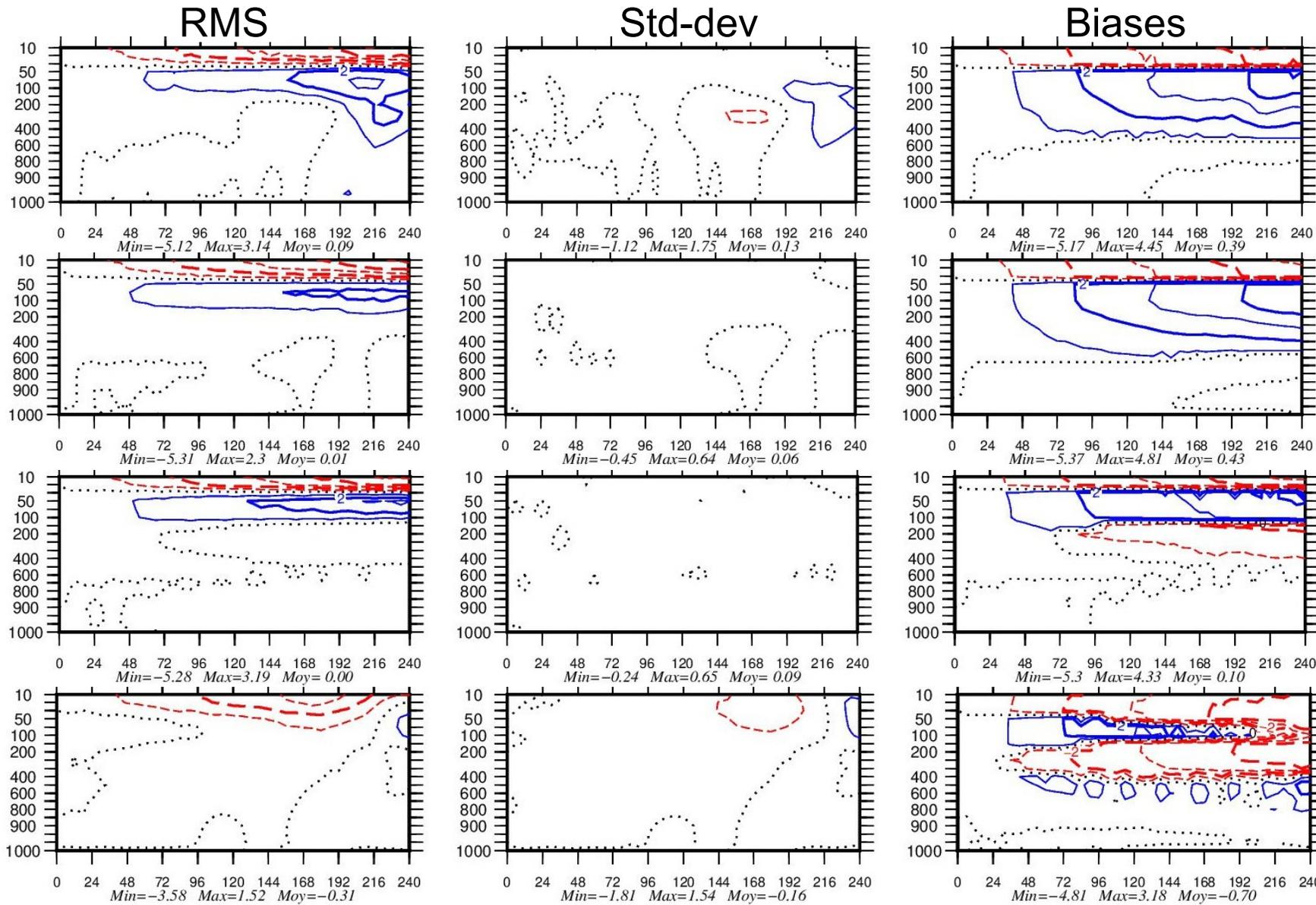
**2) Impacts of “ZDEC=0” in CPUTQY**

3) A new way to compute the mixing length “L” in “ACBL89” and “BL89”

4) Impacts of the new “L” in “ACBL89” + “BL89”

5) Conclusions

# Impacts of “ZDEC=0” all param. / Geopotential [ 51 days / 240 h / analyses ]



Scores for ARPEGE  
by **Eric Bazile**  
“blue = better  
“red” = worse  
(June/July 2020)

:EUROPE

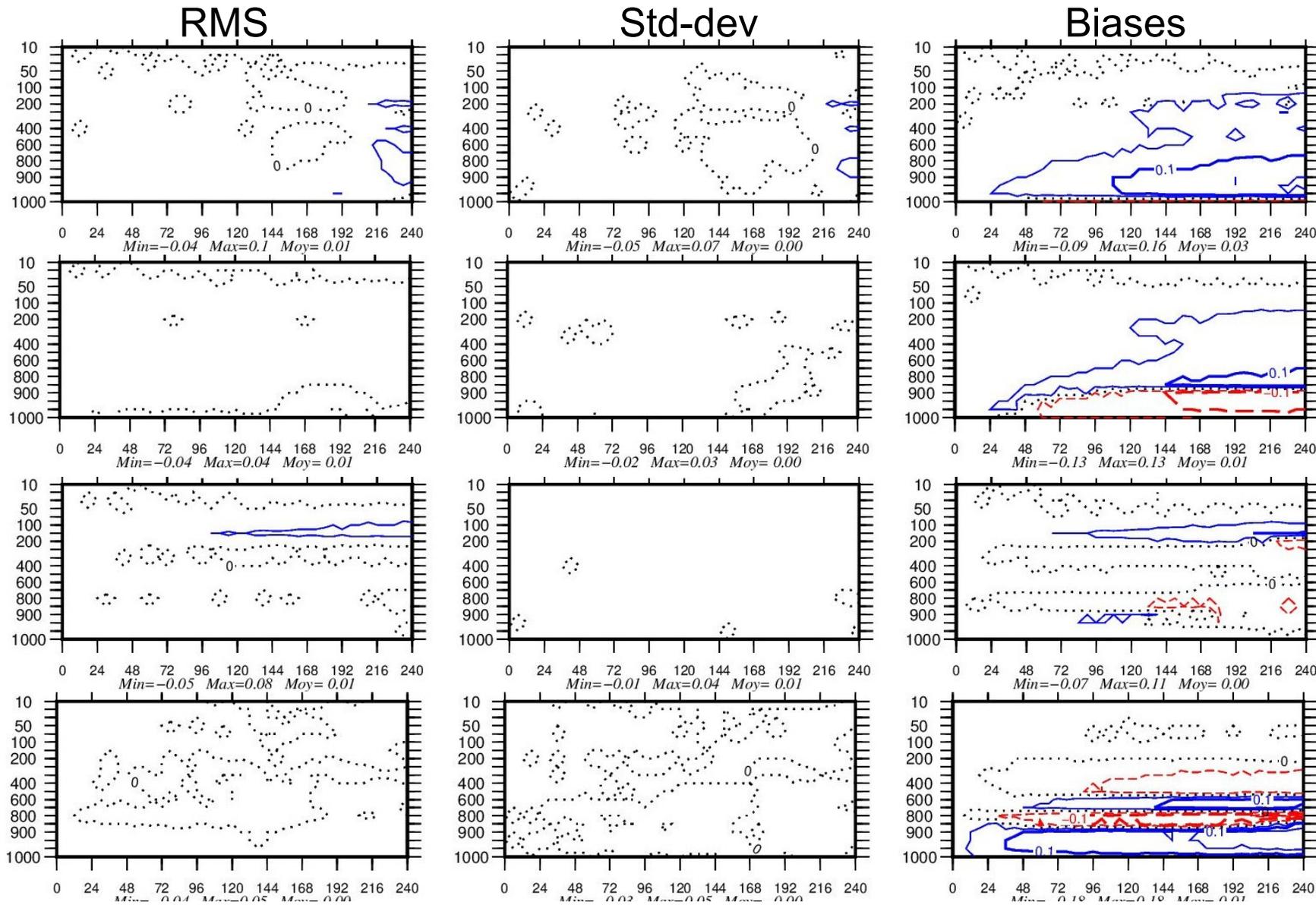
:NORTH-20N

improvements  
in Biases and RMS

:TROPICS

:SOUTH-20S

# Impacts of "ZDEC=0" all param. / Temperature [ 51 days / 240 h / analyses ]



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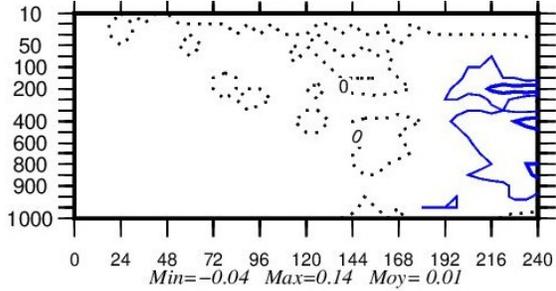
improvements  
in Biases (and RMS)

:TROPICS

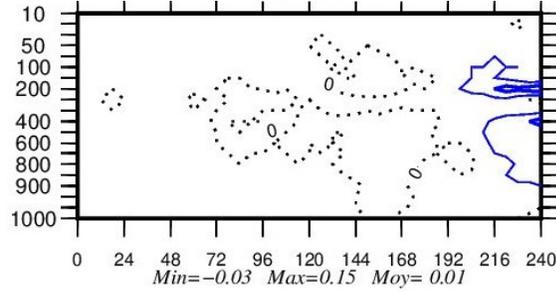
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# Impacts of “ZDEC=0” / Temperature / EUROPE [ 37 days / 240 h / analyses ]

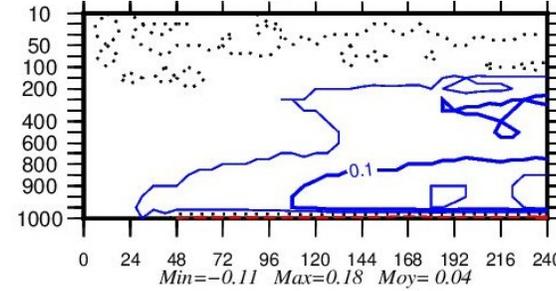
RMS



Std-dev

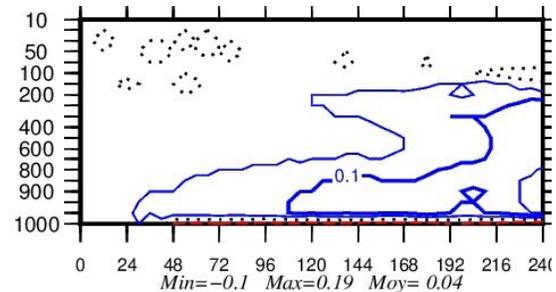
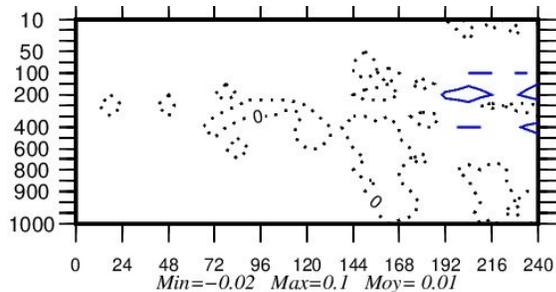
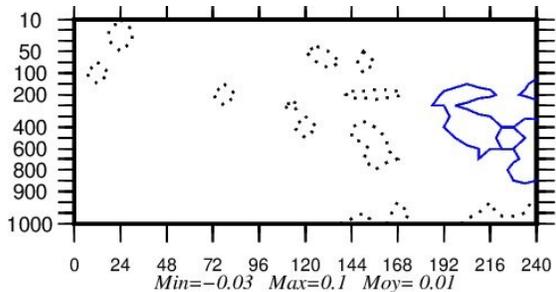


Biases



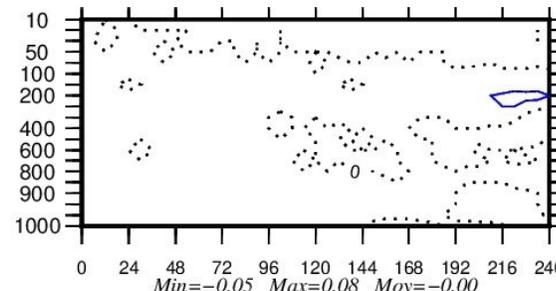
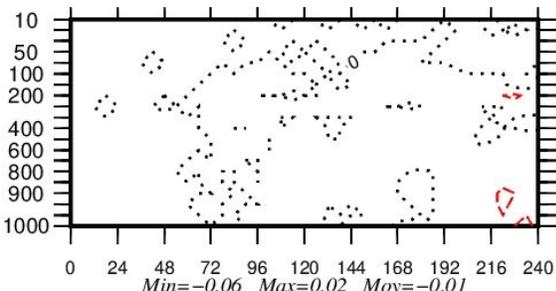
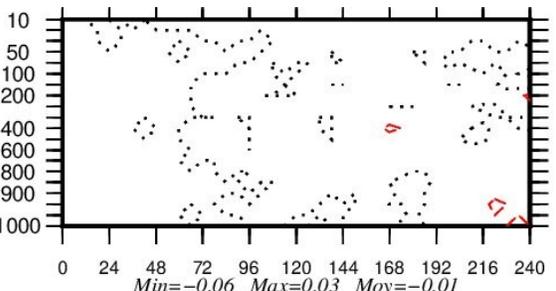
Scores for ARPEGE

all params removed in ZDEC  
by **Eric Bazile**  
“blue = better”  
“red” = worse  
(June/July 2020)



all removed in ZDEC  
**except GWD**

Small impacts of GWD alone  
(weak GWD in ARPEGE...)



all removed in ZDEC  
**except TURB**

Main impacts coming from turbulence?  
(+ links with convections)

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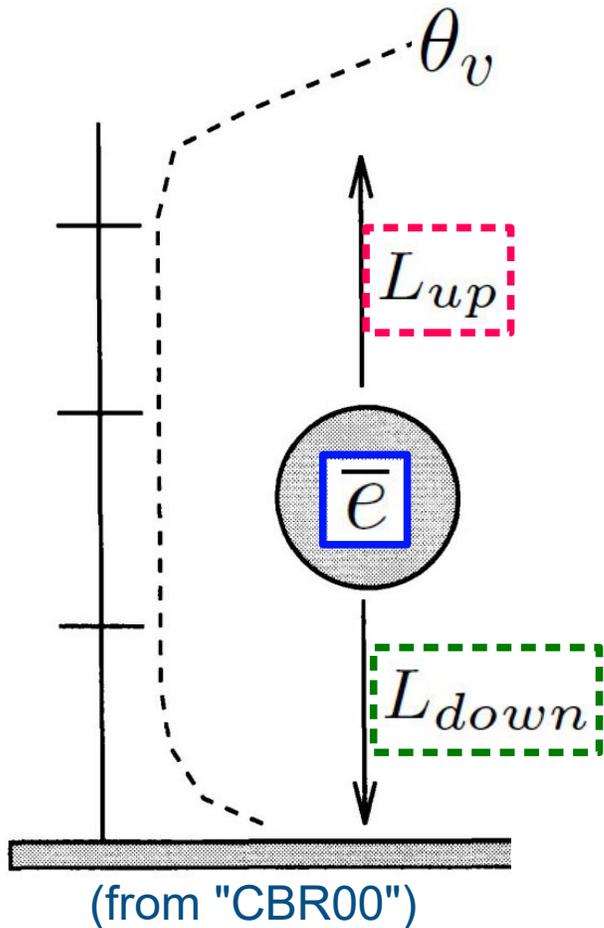
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# The "BA86" & "BL89" non-local mixing length



The vertical distances to equalize the TKE  $\bar{e}$  with the work done against buoyancy force:

$$\int_z^{z+L_{up}} \frac{g}{\theta_v} [\bar{\theta}_v(z') - \bar{\theta}_v(z)] dz' = \bar{e}$$

$$\int_{z-L_{down}}^z \frac{g}{\theta_v} [\bar{\theta}_v(z) - \bar{\theta}_v(z')] dz' = \bar{e}$$

"BA86":

$$\frac{1}{L} = \frac{1}{L_m} = \frac{1}{L_\epsilon} = \frac{1}{2} \left( \frac{1}{L_{up}} + \frac{1}{L_{down}} \right)$$

Bougeault & André (1986)

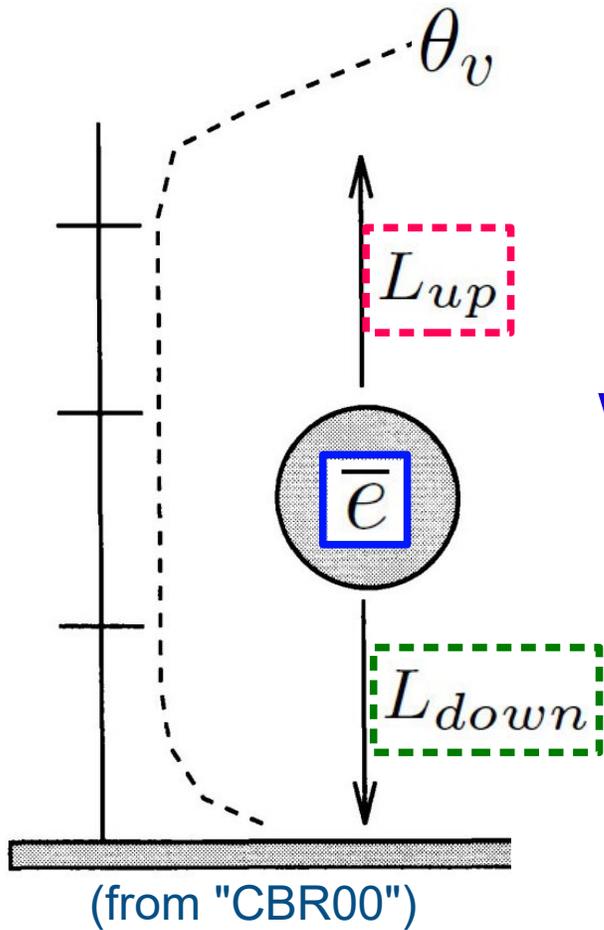
"BL89":

$$L_m = \min(L_{up}, L_{down})$$

$$L_\epsilon = \sqrt{L_{up} L_{down}}$$

Bougeault & Lacarrère (1989) (PERIDOT)

# The ARPEGE & AROME & Meso-NH non-local mixing length



present ARPEGE:  
and AROME:  
and Meso-NH:

$$\frac{1}{L^\alpha} = \frac{1}{2} \left[ \frac{1}{(L_{up})^\alpha} + \frac{1}{(L_{down})^\alpha} \right]$$

where:  $\alpha = 2/3$  and:  $L \approx 2.8 z$  Close to surface if neutral (or unstable)

(very different from the von Kármán law  $L \approx 0.4 z$ )

But why?

# The ARPEGE & AROME & Meso-NH non-local mixing length

$$\alpha = \frac{\log(16)}{4 \log(\kappa) + \log(C_\varepsilon) - 3 \log(C_m)}$$

Surface  
Neutrality:

$$L \approx A (z + z_0)$$

$$A = \kappa \frac{(C_\varepsilon)^{1/4}}{(C_m)^{3/4}}$$

Hints in RMC (2001), Lemarié *et al.* (G.M.D. 2021)

Table 1: Values of constants and derived values for different papers and models.

	BL89	Peridot	CBR00	CCH02	ARPEGE	AROME
$C_m$	0.40	0.20	0.0666667	0.1264	0.126	0.1264
$C_\varepsilon$	0.7143	0.70	0.70	0.845	0.8475	0.85
$A = \kappa (C_\varepsilon / C_m^3)^{1/4}$	0.73	1.22	2.79	1.809	1.815	1.812
$\alpha = \ln(2) / \ln(A)$	-2.21	3.44	0.676 $\approx$ 2/3	1.1692 $\approx$ 7/6	1.1631	1.1663

(0.6666...)  $\alpha \approx 2/3$

Still  $\alpha \approx 2/3$  ! should be  $\alpha \approx 7/6$  !  
(0.6666...) (1.16666...)

With "A" reduced from 2.8 to 1.8  
→ reduced surface fluxes?

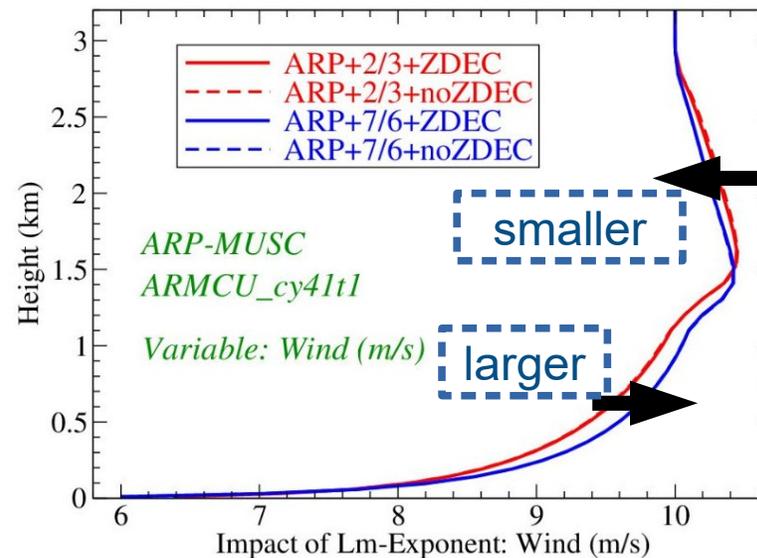
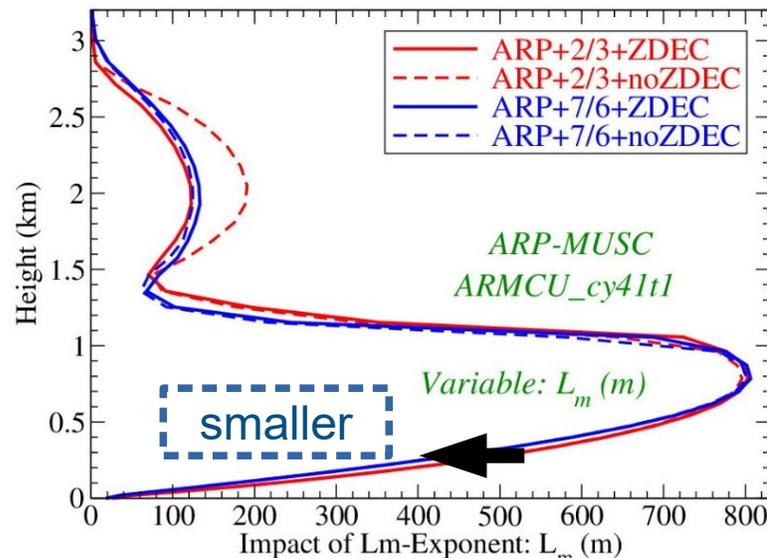
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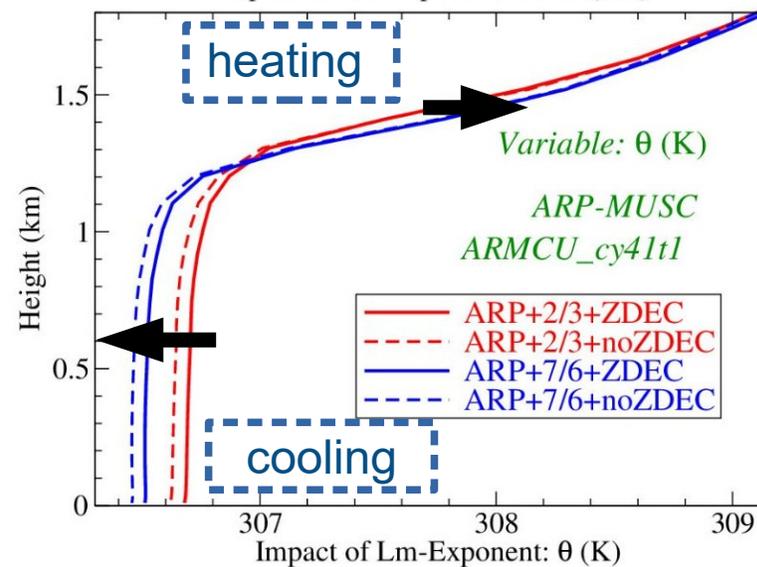
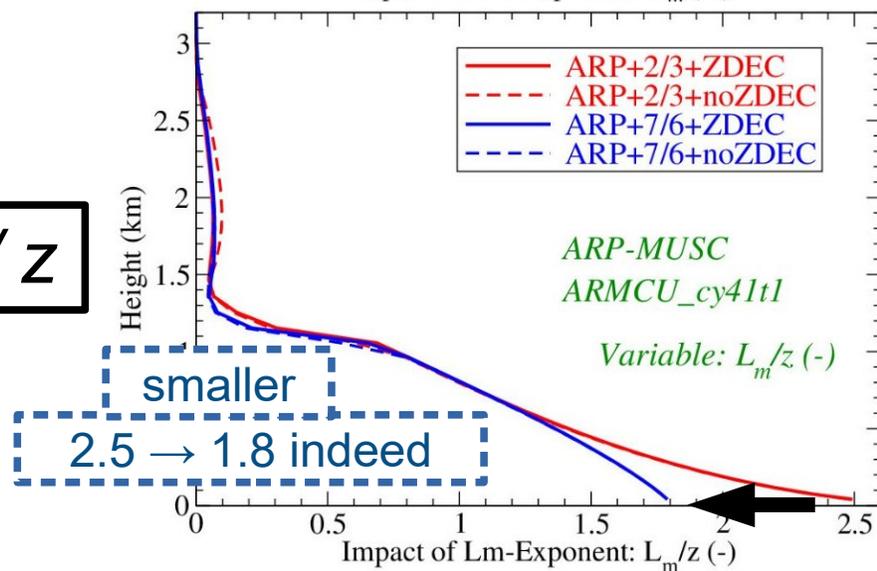
# Impacts of “L”: “2/3” → “7/6” ( “ACBL89” ARPEGE MUSC-1D ARM-Cumulus)

**L**



**||v||**

**L/z**



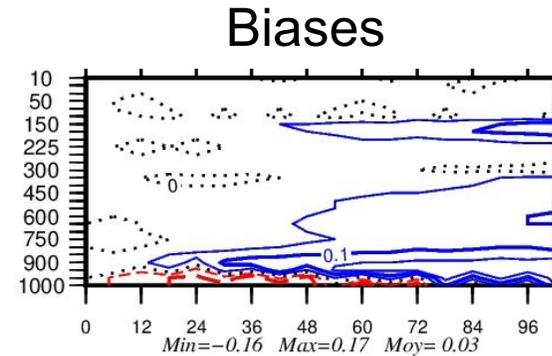
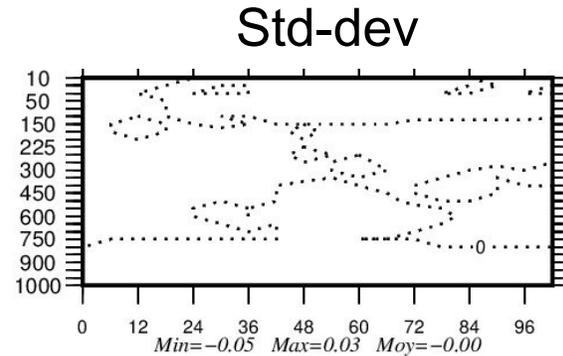
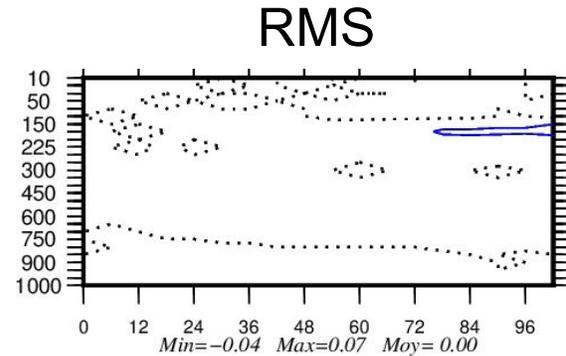
**$\theta$**

# Impacts of the new “L” with “7/6” in “ACBL89” (ARPEGE)

## Temperature [ 44 days / 96 h / analyses ]

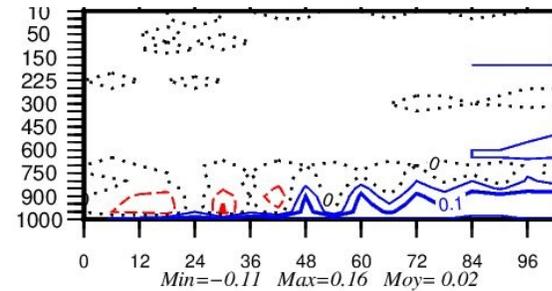
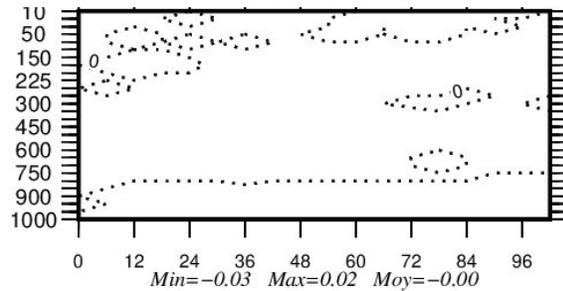
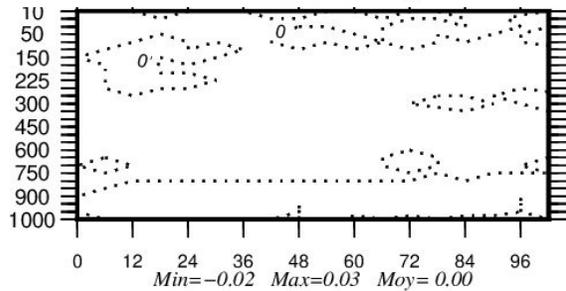
“blue = better  
“red” = worse

(Jan./Feb. 2021)



EUROPE

improvements  
(cooling)



NORTH-20N

improvements  
(cooling)

## Impacts of the new “L” with “7/6” in “ACBL89 / BL89”

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Jean-François Gueremy (ARPEGE / Seasonal-Forecast / 5 years coupled AOGCM)

- smaller surface fluxes
- E and P: from 3.17 to 3.09 mm/day
- reduced “warm bias” in continental Europe (JJA)

Yann Seity (AROME-NWP / 1 month 3DVar)

- neutral classical scores (u, v, T, HU)
- neutral precipitation and gustiness scores

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# Conclusions

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- 1) To be aware that “ **$C_p T$** ” or “**Moist Static Energies**” are neither enthalpy nor energy  
“ **$C_p T$** ” or “ **$C_p T + K$** ” or “**MSE**” might be conserved and not energy, and vice versa!

The safer method is likely the simplest: update the basic variables (“ $u$ ”, “ $v$ ”, “ **$C_p T$** ”),  
→ this is done with “**ZDEC=0**”

# Conclusions

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“ **$C_p T$** ” or “ **$C_p T + K$** ” or “**MSE**” might be conserved and not energy, and vice versa!

The safer method is likely the simplest: update the basic variables (“ $u$ ”, “ $v$ ”, “ **$C_p T$** ”),  
→ this is done with “**ZDEC=0**”

- 2) A need to change “alpha ( $C_m, C_\epsilon$ )” in ARPEGE, AROME, Meso-NH, ... (“BA/BL” codes)

A need to maintain competence in turbulence, and likely to revisit the CBR scheme

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***Thanks! Questions ?***

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